

REAL TIME MODEL-CHECKING AND UPPAAL

FLORIAN LORBER

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Florian Lorber
Silicon Austria Labs
(Slides from Aalborg University)



MODEL CHECKING

- ≡ Bring me up to speed about what you know
- ≡ Check whether a model fulfills certain properties
 - ≡ Does our robot behave like a human?
- ≡ What kind of properties can you check?
- ≡ What are the two biggest problems with model-checking?



PROPERTIES

≡ Functional correctness

- ≡ Does the system do what it is supposed to?

≡ Reachability

- ≡ Is it possible to end up in a certain state?
- ≡ Can the robot set itself on fire?

≡ Safety

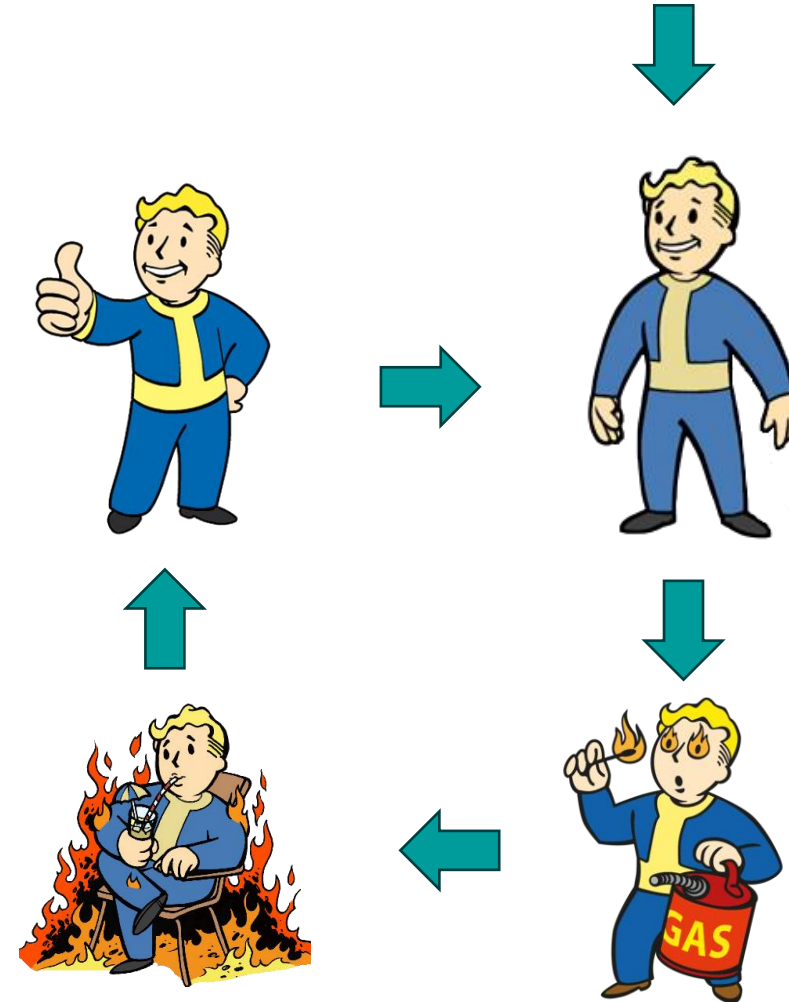
- ≡ Something bad can never happen
- ≡ Will the robot never die?

≡ Liveness

- ≡ Something good will eventually happen
- ≡ Will the robot recover?

≡ Fairness

- ≡ In cert. conditions, can an event occur repeatedly
- ≡ Will the robot always recover?



STRENGTHS OF MODEL CHECKING

- ≡ General verification technique
- ≡ Partial verification is possible
- ≡ Covers all traces
- ≡ Sound and mathematical foundation
- ≡ My highlights about model-checking from papers:
 - ≡ “No high degree of expertise needed”
 - ≡ “Learning curve is not steep”



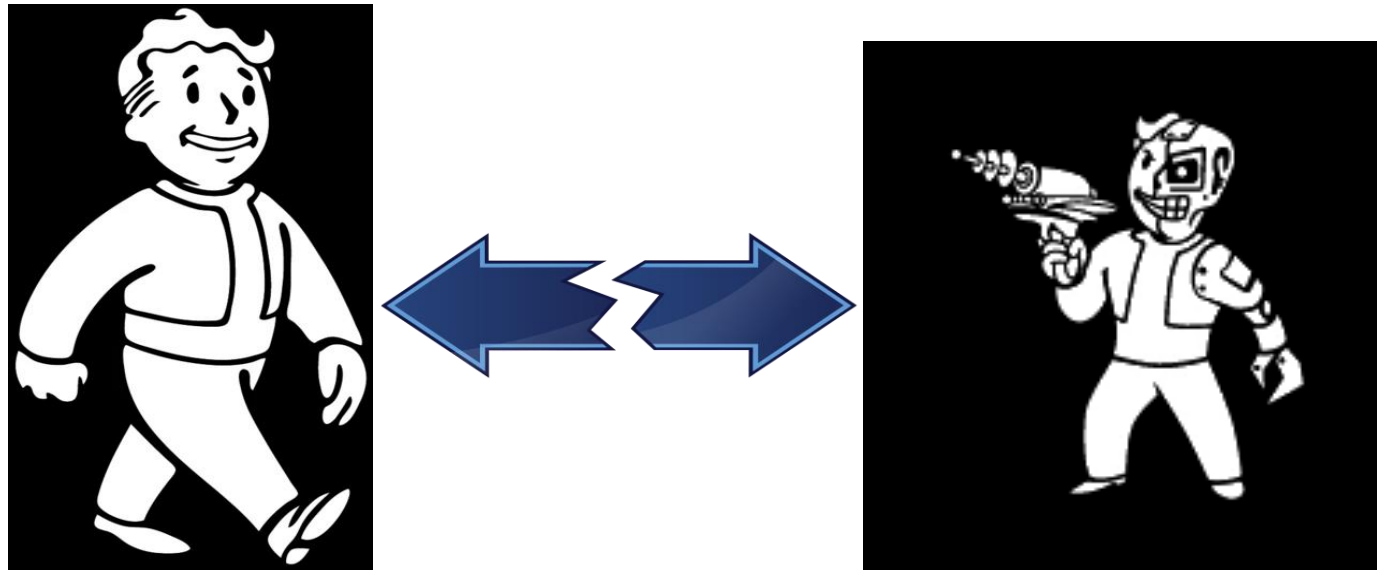
WEAKNESSES

- ≡ Not for data intensive applications
- ≡ Decidability issues
- ≡ Only the model is verified
- ≡ State space explosion



MODELLING GAP

- Any verification using model-based techniques is only as good as the model of the system.



STATE SPACE EXPLOSION

- ≡ Too many states to complete the verification
- ≡ Concurrency, Data Variables, Complexity, ...
- ≡ Consequences:
 - ≡ Memory consumption
 - ≡ Computation time
 - ≡ Scalability



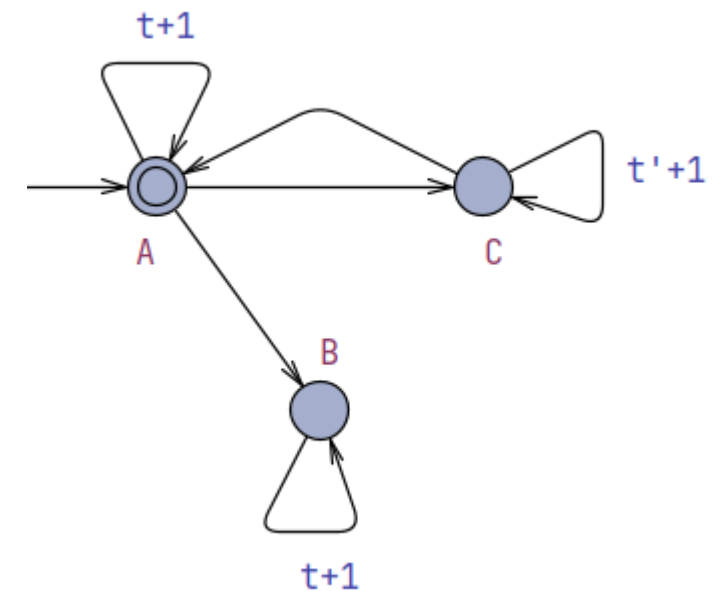
REAL TIME SYSTEMS

- ≡ Systems with Soft and Hard Deadlines
- ≡ Soft Deadline:
 - ≡ Some degree for flexibility
 - ≡ Missed deadline leads to degraded performance
- ≡ Hard Deadline:
 - ≡ No exceptions
 - ≡ Missed deadline leads to catastrophic failures
 - ≡ E.g. Pacemaker, traffic control, etc.



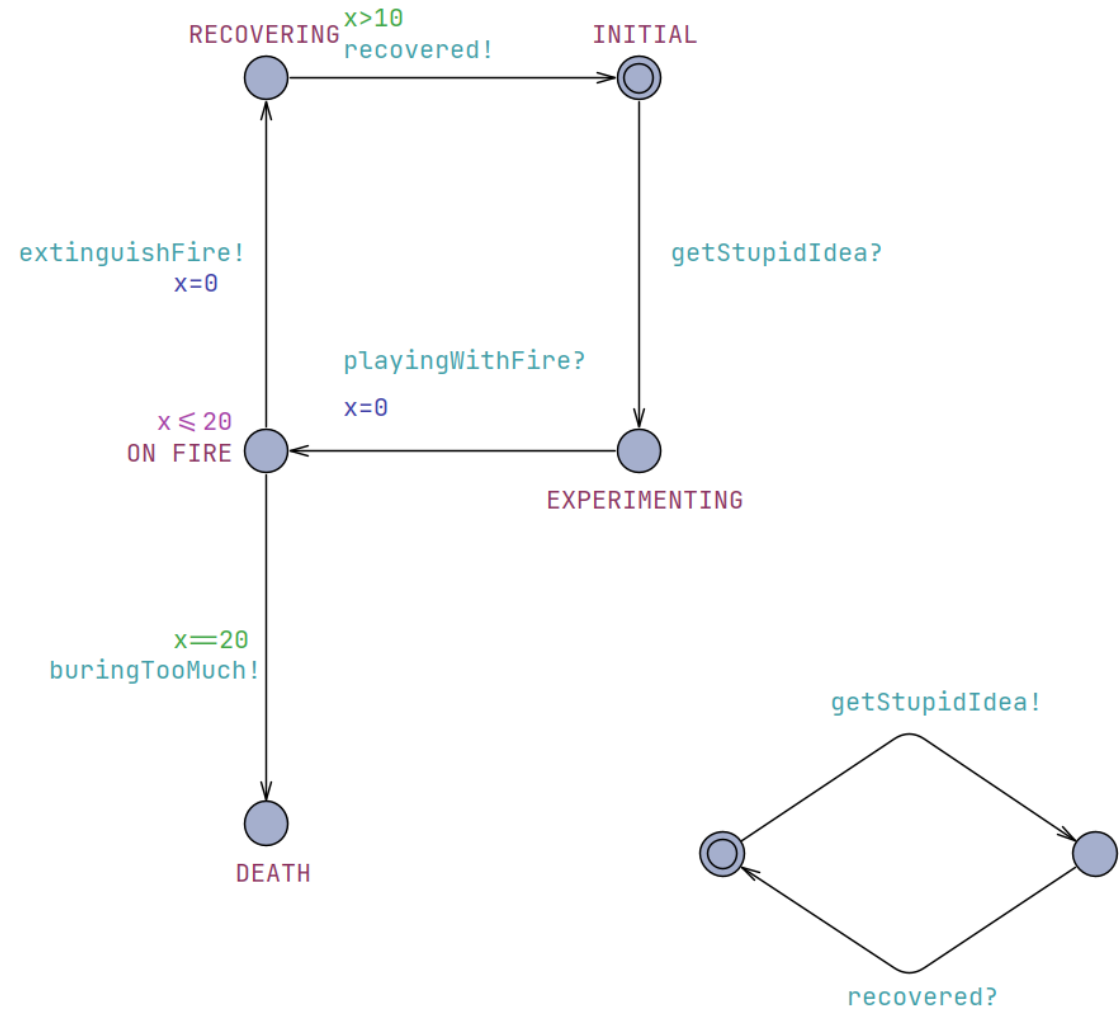
REAL TIME SYSTEMS

- ≡ Why does time warrant for each own lecture?
- ≡ I want to enter state B 5 seconds after I enter state A
 - ≡ How many variables needed to keep track of the timing?
 - ≡ What if time I spend in state C does not count to the 5 seconds?
- ≡ Consider discrete time
 - ≡ Time can count up in each state
- ≡ Now imagine the state space with real variables



TIMED AUTOMATA

- ≡ Extended final state machine
 - ≡ Labeled transitions
 - ≡ Clock variables
 - ≡ Measures continuous time
- ≡ Time progresses in locations
 - ≡ There might be a time limit
- ≡ Actions are instantaneous
 - ≡ Might only be enabled in certain times
 - ≡ Can reset clocks
- ≡ Networks of timed automata
 - ≡ ?!
- ≡ Statespace?



TIMED AUTOMATA - FORMAL

- ≡ Set of clocks C
- ≡ $B(C)$ is the set of junctions of simple conditions
 - ≡ $x \{<, \leq, =, \geq, >\} c$
 - ≡ $x - y \{<, \leq, =, \geq, >\} c$
 - ≡ $x, y \in C, c \in \mathbb{N}$
- ≡ Set of clock valuations v
- ≡ Valuations map clocks to real values
- ≡ $v(x) \rightarrow \mathbb{R}$

- ≡ Timed Automaton: $TA = (L, l_0, C, A, E, I)$
- ≡ L : set of locations
- ≡ l_0 : initial location
- ≡ C : set of clocks
- ≡ A : set of actions
- ≡ E : set of edges
 - ≡ $E \subseteq L \times A \times B(C) \times 2^C \times L$
- ≡ $I : L \rightarrow B(C)$

- ≡ Semantics:

- ≡ Clock valuations v
- ≡ Map clocks to real values
- ≡ $v(x) \rightarrow \mathbb{R}$
- ≡ $v_0(x) \rightarrow 0 \forall x \in C$

Definition 2 (Semantics of TA). Let (L, l_0, C, A, E, I) be a timed automaton. The semantics is defined as a labelled transition system $\langle S, s_0, \rightarrow \rangle$, where $S \subseteq L \times \mathbb{R}^C$ is the set of states, $s_0 = (l_0, u_0)$ is the initial state, and $\rightarrow \subseteq S \times \{\mathbb{R}_{\geq 0} \cup A\} \times S$ is the transition relation such that:

- $(l, u) \xrightarrow{d} (l, u + d)$ if $\forall d' : 0 \leq d' \leq d \implies u + d' \in I(l)$, and
- $(l, u) \xrightarrow{a} (l', u')$ if there exists $e = (l, a, g, r, l') \in E$ s.t. $u \in g$, $u' = [r \mapsto 0]u$, and $u' \in I(l')$,

UPPAAL - OUTLINE

- ≡ GUI
- ≡ Modelling language
- ≡ Simulator
- ≡ Formal semantics
- ≡ Query language
- ≡ Reachability algorithm

GUI - DEMO

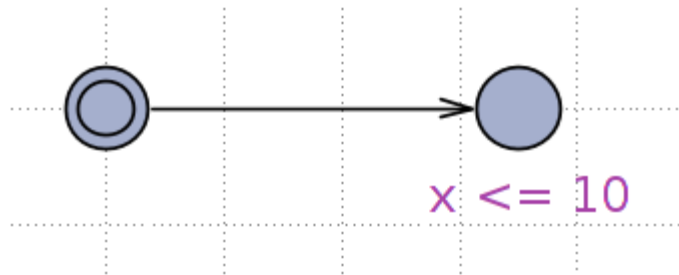
Automaton, Location, Edge, Synchronization, Guard,
Update, Select, Clocks, Channels, Environment, System
Declarations, Simulator

NOTATION

- ≡ Location – a place in a single template or process
- ≡ State – the state of the complete system including clock valuations and variable values
- ≡ Edge – a step between two locations
- ≡ Transition – a change of the global state of the system

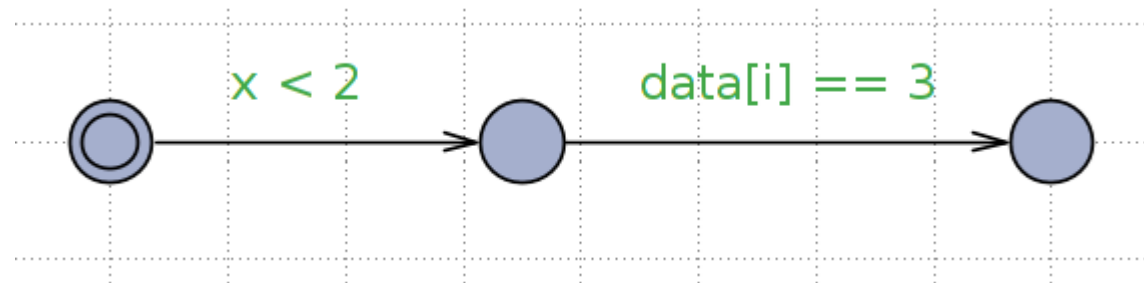
INVARIANT

- ≡ Something that must be true in a given location
- ≡ If it is not true we must leave or else we deadlock
- ≡ If it is not true we cannot enter the location



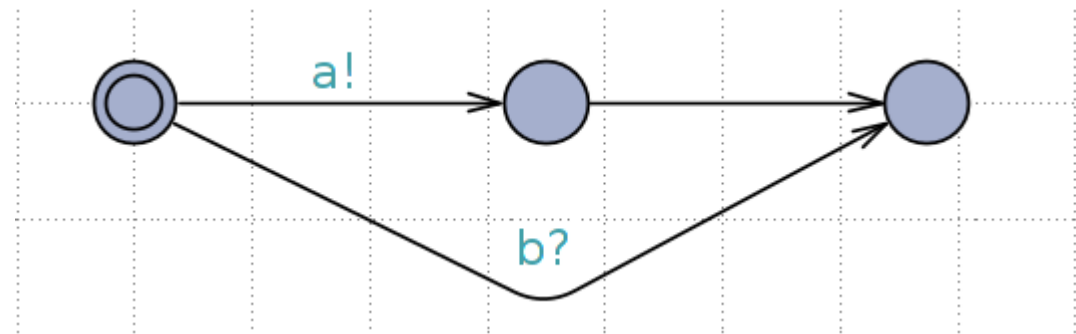
GUARD

A condition that must be true in order for an edge to be enabled



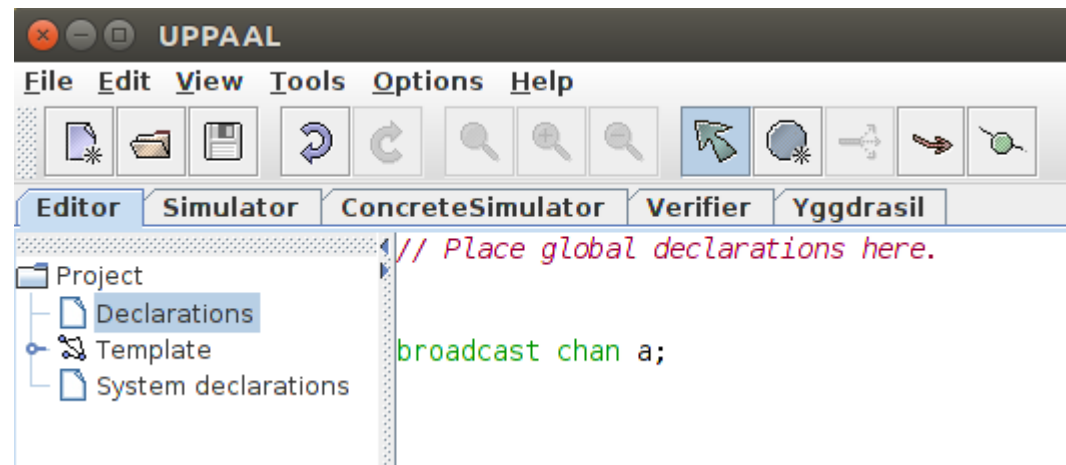
SYNCHRONIZATION

- ≡ The label on which the edge synchronizes with another edge
- ≡ If nothing is present
 - ≡ We call it a Tau τ / silent / epsilon ε transition
 - ≡ Can be taken alone



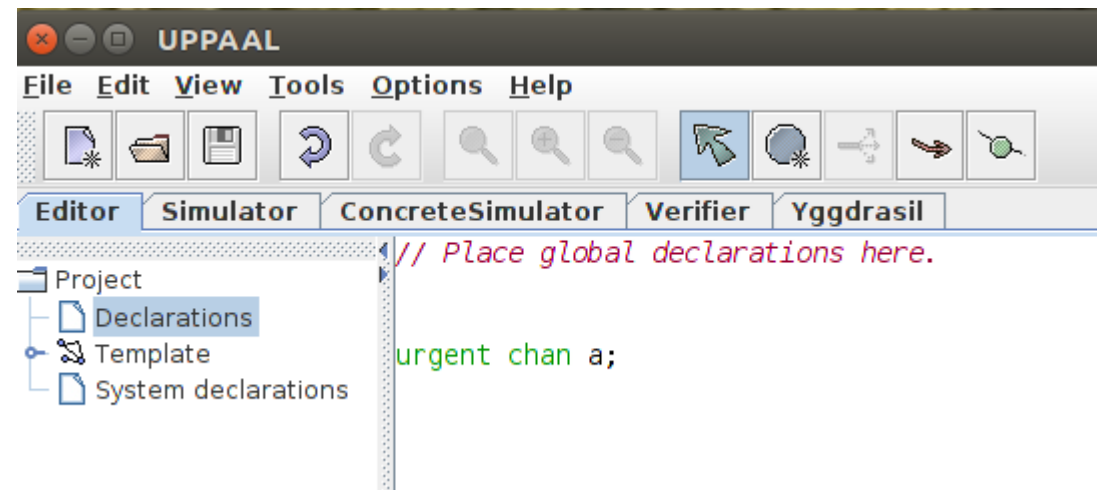
BROADCAST CHANNELS

- ≡ One sender
- ≡ Multiple receivers
 - ≡ All that can participate must participate
 - ≡ Note: Invariants after the input can block the execution of the complete broadcast



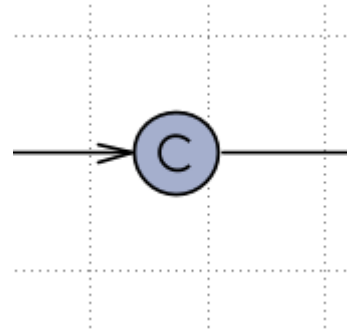
URGENT CHANNELS

- ≡ Must synchronize on an urgent channel as soon as it is possible
- ≡ Does not allow clock guards on edges that synchronize on urgent channels
- ≡ Data guards on the receiver can be a problem



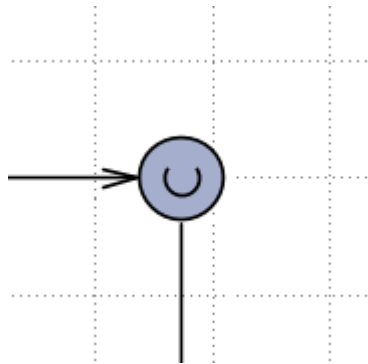
COMMITTED LOCATION

- ≡ Time must not pass while this location is part of the global state
- ≡ If there is any committed location among the locations in the global state then the next transition must involve at least one committed location



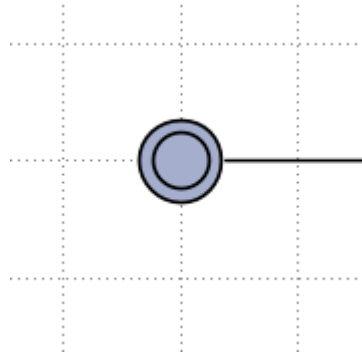
URGENT LOCATION

≡ Time must not pass while this location is part of the global state

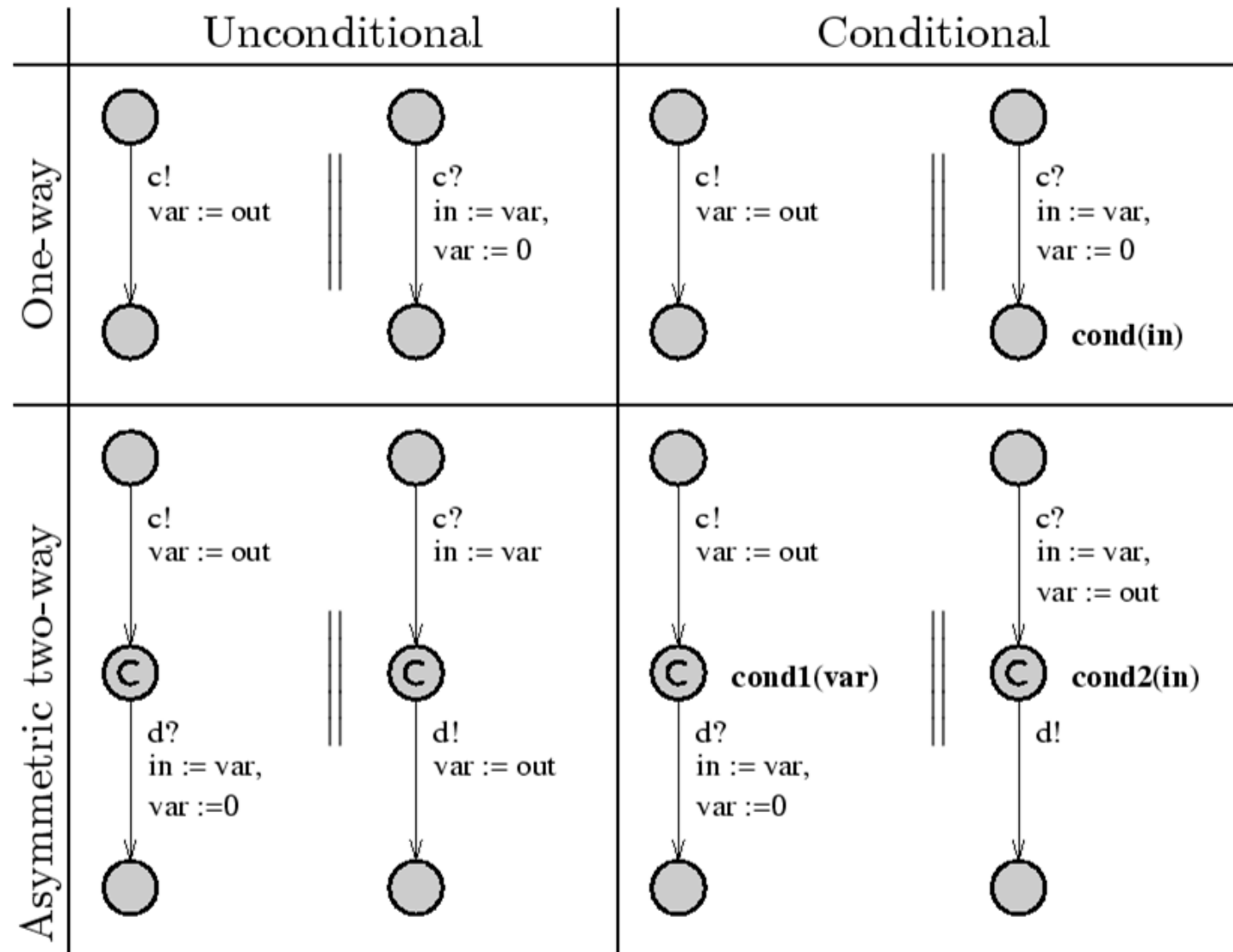


INITIAL LOCATION

≡ The location in which a given process starts



SYNCHRONOUS VALUE PASSING



MODELLING LANGUAGE

MODELING LANGUAGE

- Global and local definitions, and system declaration
- Types
 - built-in types: *int*, *int[min,max]*, *bool*, arrays
 - *typedef struct { ... } name*
 - *typedef built-in-type name*
- Functions
 - C-style syntax, no pointer, can load C libraries
- Select
 - *name : type*
- Network of TA = instances of templates
 - argument *const type expression*
 - argument *type& name*

EXAMPLE: FREE PIZZA STOPWATCH

- Hit the stop button at exactly 10 seconds for pizza
- Two systems: watch and user
- Signals: Start, stop, tooLate, tooEarly, reward
- After the reward, the user shouts “freePizzzzzza” into the world
- Global variable for coins, 10 coins as reward
 - Change model so that a pizza costs 20 coins
 - You need to hit the button twice
- Use concrete and symbolic simulation



Youtube screenshot

SPECIFICATION LANGUAGE

LOGICAL SPECIFICATIONS

■ Validation Properties

–Possibly: $E \leftrightarrow P$

■ Safety Properties

–Invariant: $A[] P$

–Pos. Inv.: $E[] P$

■ Liveness Properties

–Eventually: $A \leftrightarrow P$

–Leadsto: $P \rightarrow Q$

■ Bounded Liveness

–Leads to within: $P \rightarrow_{\leq t} Q$

≡ The expressions P and Q must be type safe, **side effect free**, and evaluate to a boolean.

≡ Only references to integer variables, constants, clocks, **and locations** are allowed (and arrays of these).

SYMBOLS

- \exists = exists = there is one path
- \forall = forall = for all paths
- \square = Always = The whole path
- \diamond = Eventually = At some point along the path

LOGICAL SPECIFICATIONS

■ Validation/Reachability Properties

–Possibly: $E \leftrightarrow P$

■ Safety Properties

–Invariant: $A[] P$

–Pos. Inv.: $E[] P$

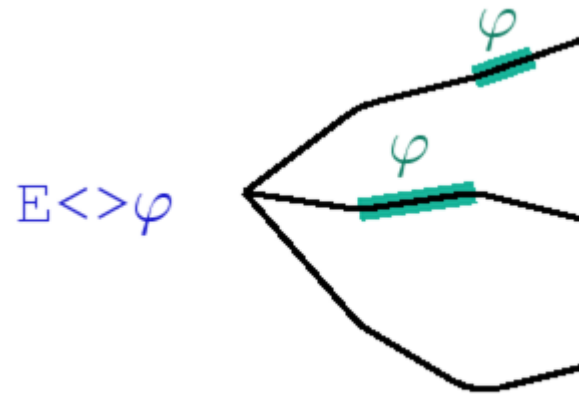
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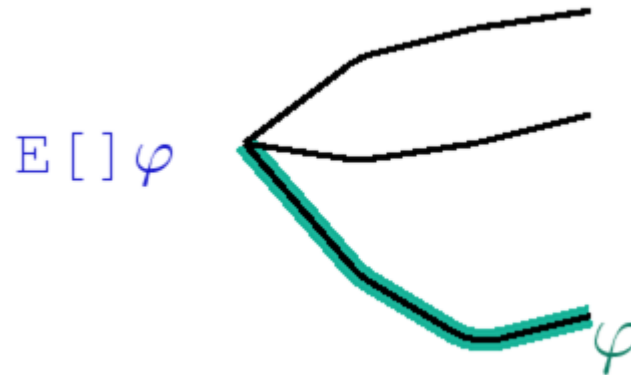
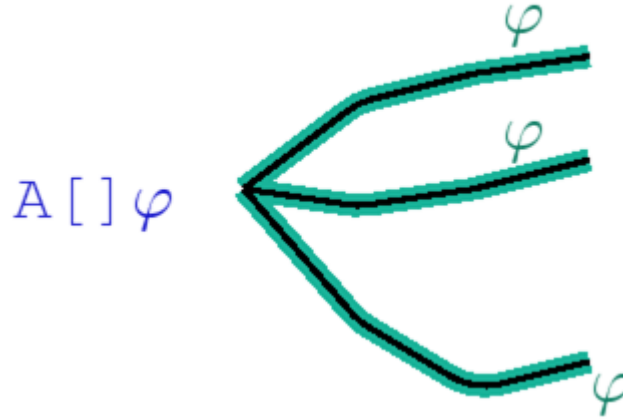
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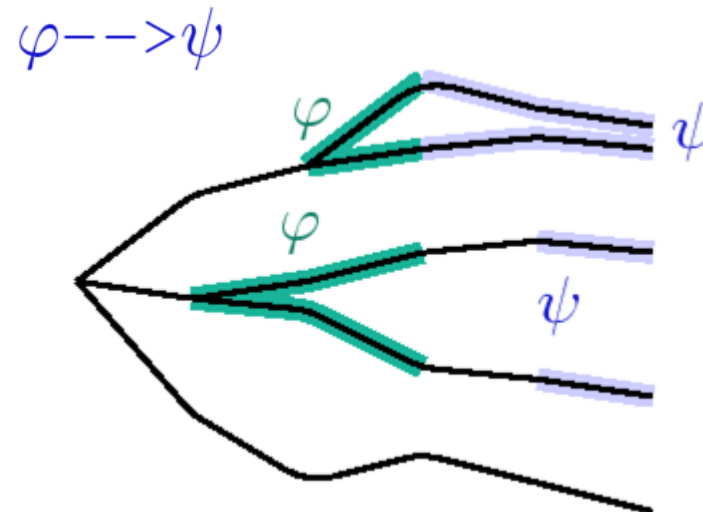
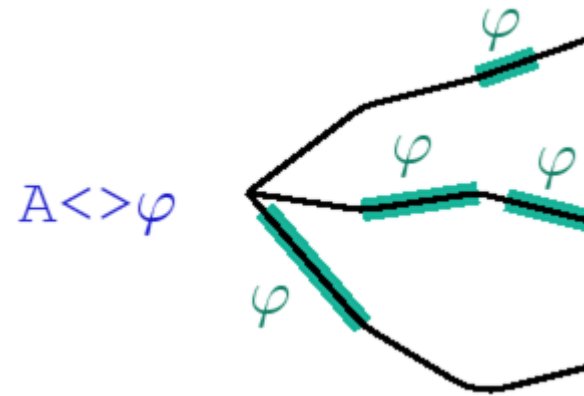
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LOGICAL SPECIFICATIONS

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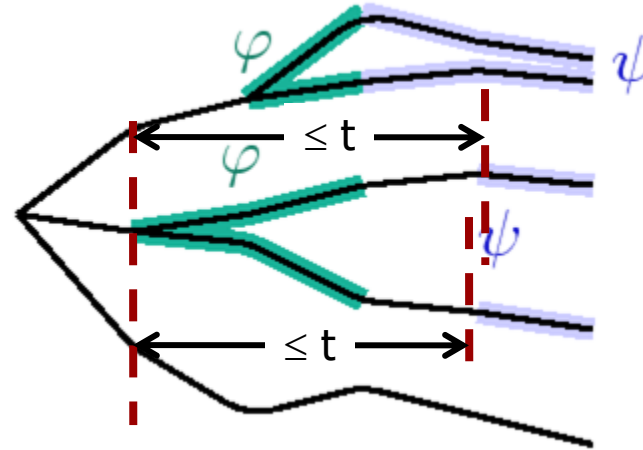
■ Liveness Properties

-Eventually: $A \langle \rangle P$

-Leadsto: $P \rightarrow Q$

■ Bounded Liveness

-Leads to within: $P \rightarrow_{\leq t} Q$



STOPWATCH EXAMPLE

- Safety: Do debt allowed

– $A[] \text{ coins} \geq 0$

- Validation/Reachability: We do not cheat

– $E \leftrightarrow \text{coins} \Rightarrow 10$

- Try it out:

– Can you think of more queries?

– Make some queries that (should) fail

QUESTIONS

- ≡ What is the difference between an urgent location and an urgent channel?
- ≡ What is the difference between a committed and an urgent location?
- ≡ What is the difference between location and a state? And why do we care?
- ≡ How can I check if a model never reaches a certain state?
- ≡ How to check for deadlock freeness?

UPPAAL VERIFICATION ENGINE

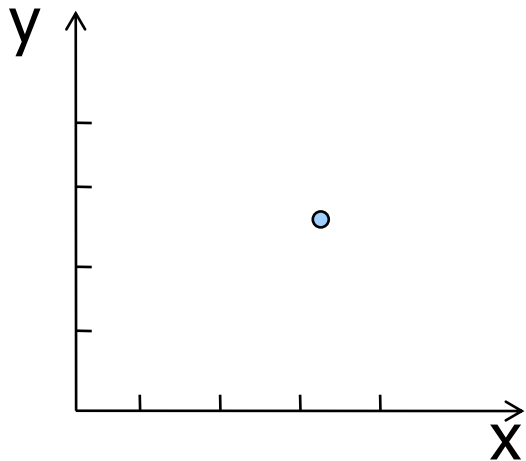
STATE-SPACE EXPLOSION PROBLEM

- ≡ 10 (11) components with 2 states each
 - ≡ $2^{10} = 1024$ states
 - ≡ $2^{11} = 2048$ states
- ≡ 2 (3/9) components with 10 states each
 - ≡ $10^2 = 100$ states
 - ≡ $10^3 = 1000$ states
 - ≡ $10^9 = 1000000000$ states

ZONES - FROM INFINITE TO FINITE

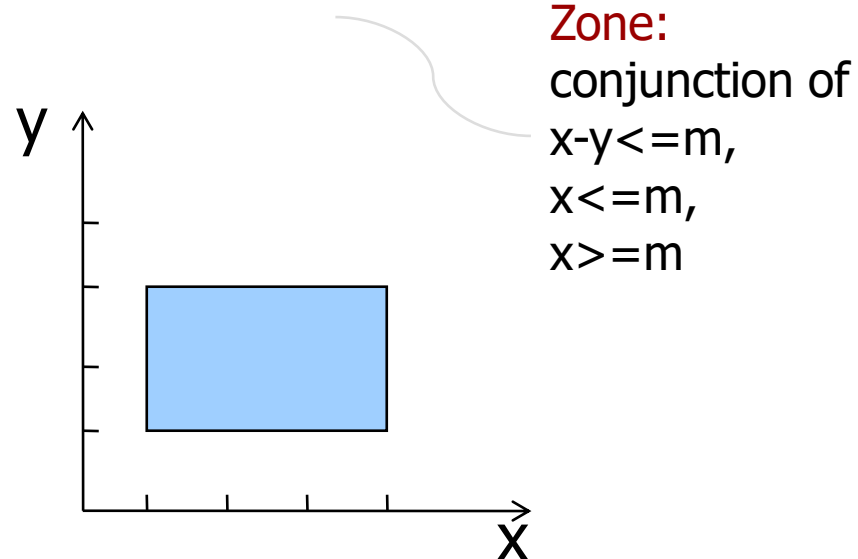
State

$(n, x=3.2, y=2.5)$

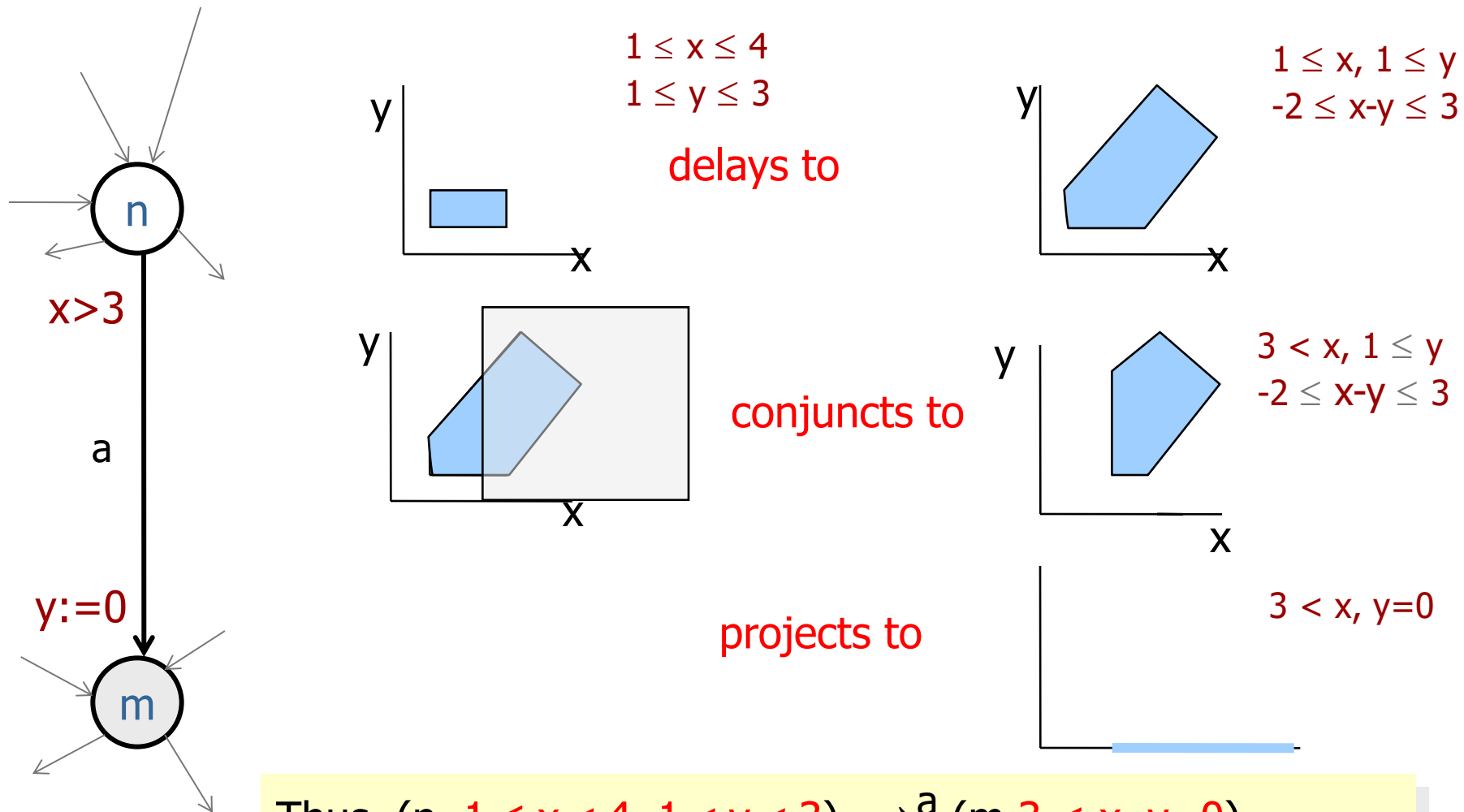


Symbolic state (set)

$(n, 1 \leq x \leq 4, 1 \leq y \leq 3)$



SYMBOLIC TRANSITIONS

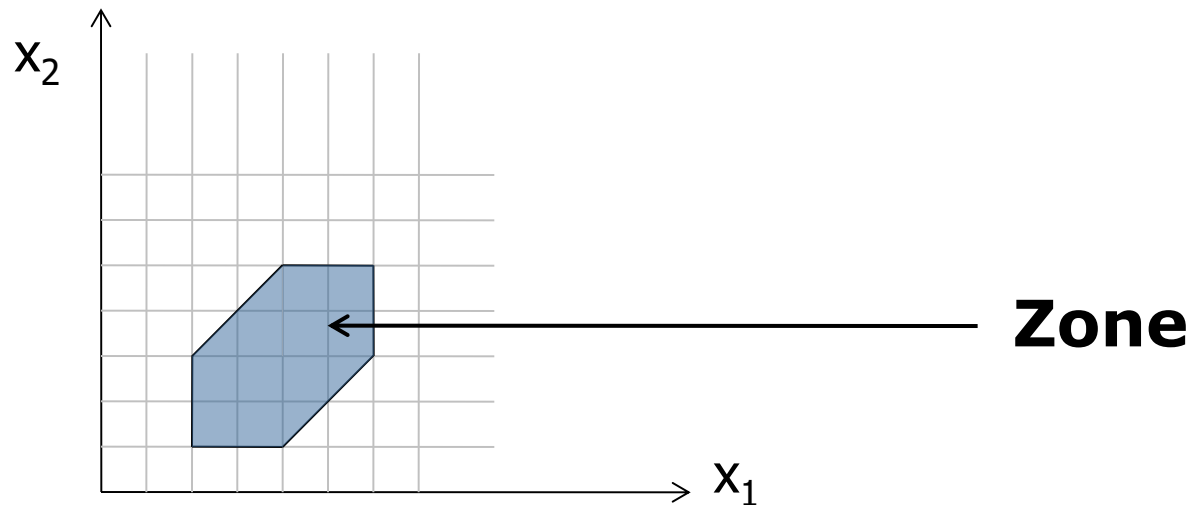


Thus $(n, 1 \leq x \leq 4, 1 \leq y \leq 3) \xrightarrow{a} (m, 3 < x, y = 0)$

DIFFERENCE BOUND MATRICES

$x_0 - x_0 \leq 0$	$x_0 - x_1 \leq -2$	$x_0 - x_2 \leq -1$
$x_1 - x_0 \leq 6$	$x_1 - x_1 \leq 0$	$x_1 - x_2 \leq 3$
$x_2 - x_0 \leq 5$	$x_2 - x_1 \leq 1$	$x_2 - x_2 \leq 0$

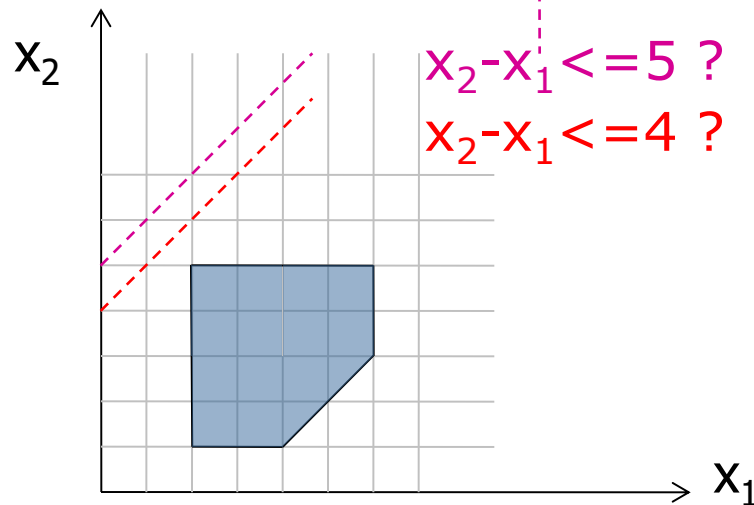
$$\mathbf{x}_i - \mathbf{x}_j \leq \mathbf{c}_{ij}$$



DIFFERENCE BOUND MATRICES

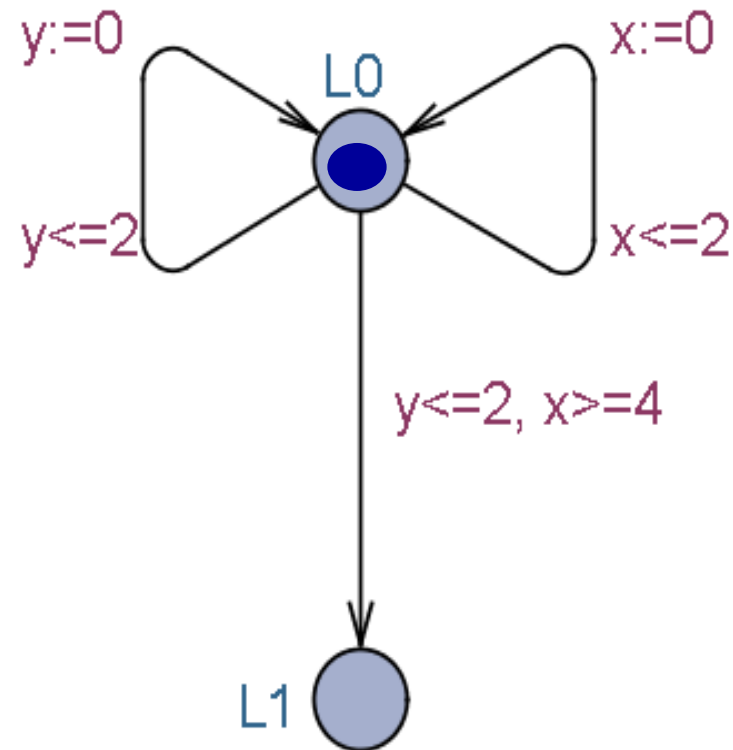
$x_0 - x_0 \leq 0$	$x_0 - x_1 \leq -2$	$x_0 - x_2 \leq -1$
$x_1 - x_0 \leq 6$	$x_1 - x_1 \leq 0$	$x_1 - x_2 \leq 3$
$x_2 - x_0 \leq 5$	$x_2 - x_1 \leq \mathbf{3}$	$x_2 - x_2 \leq 0$

$$\mathbf{x_i - x_j \leq c_{ij}}$$

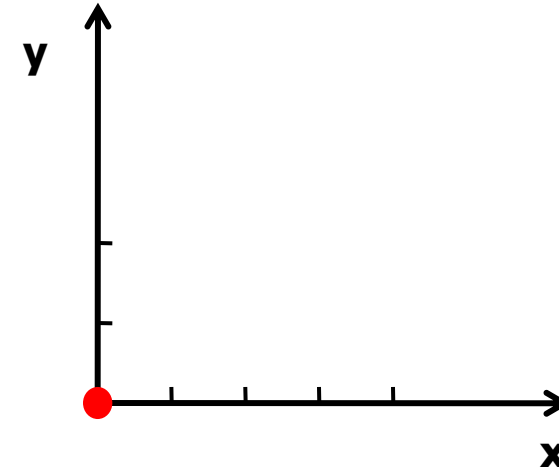


Canonical representation:
All constraints **as tight as possible**.
Needed for **inclusion checking**.
→ **Unique** DBM to represent a zone.

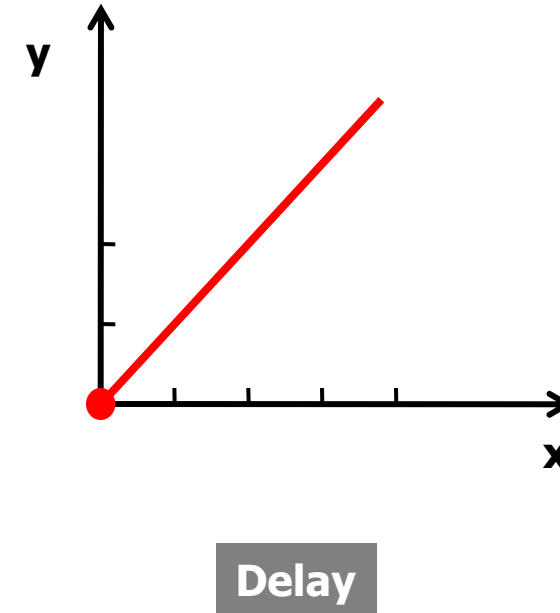
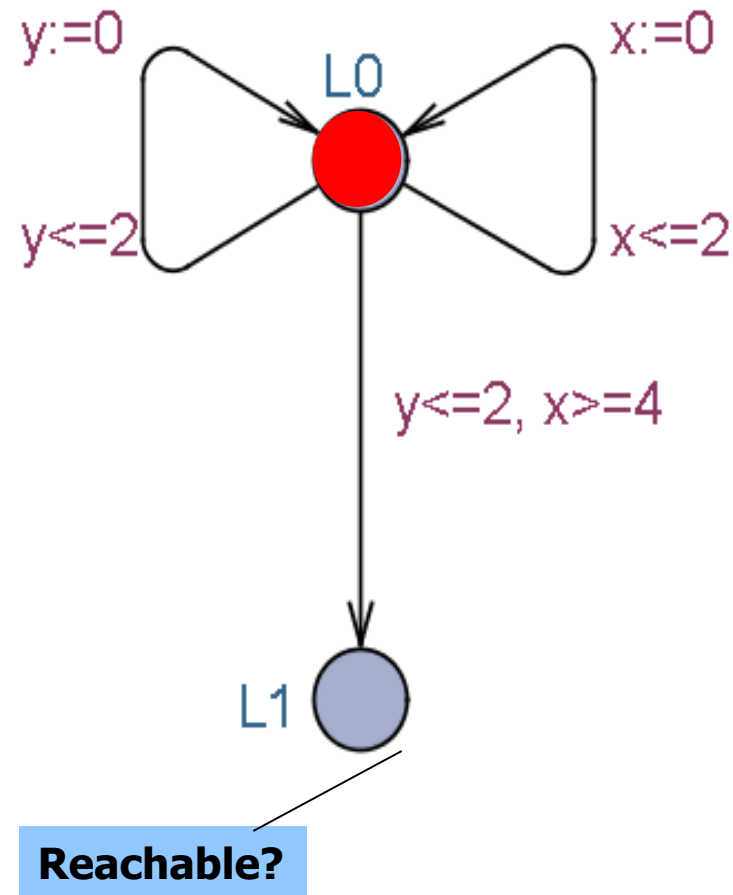
SYMBOLIC EXPLORATION



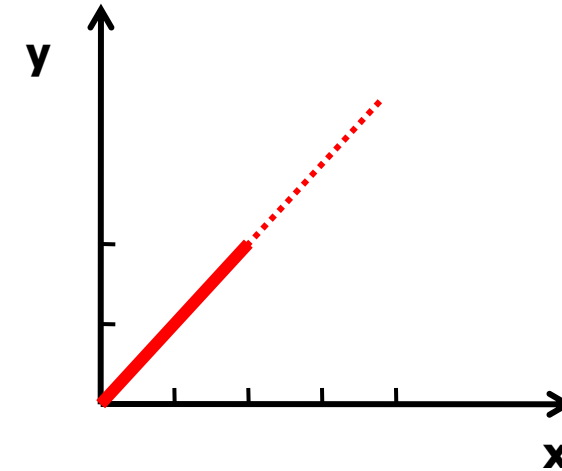
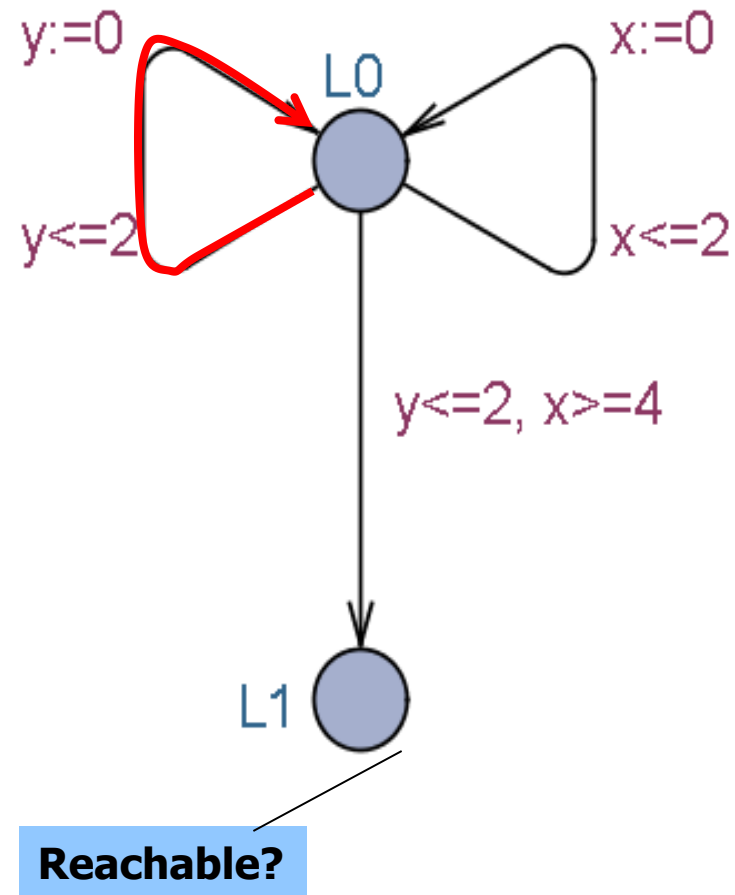
Reachable?



SYMBOLIC EXPLORATION

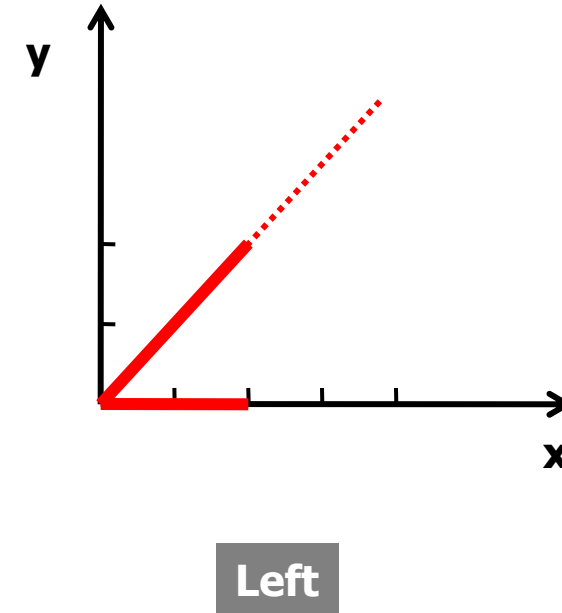
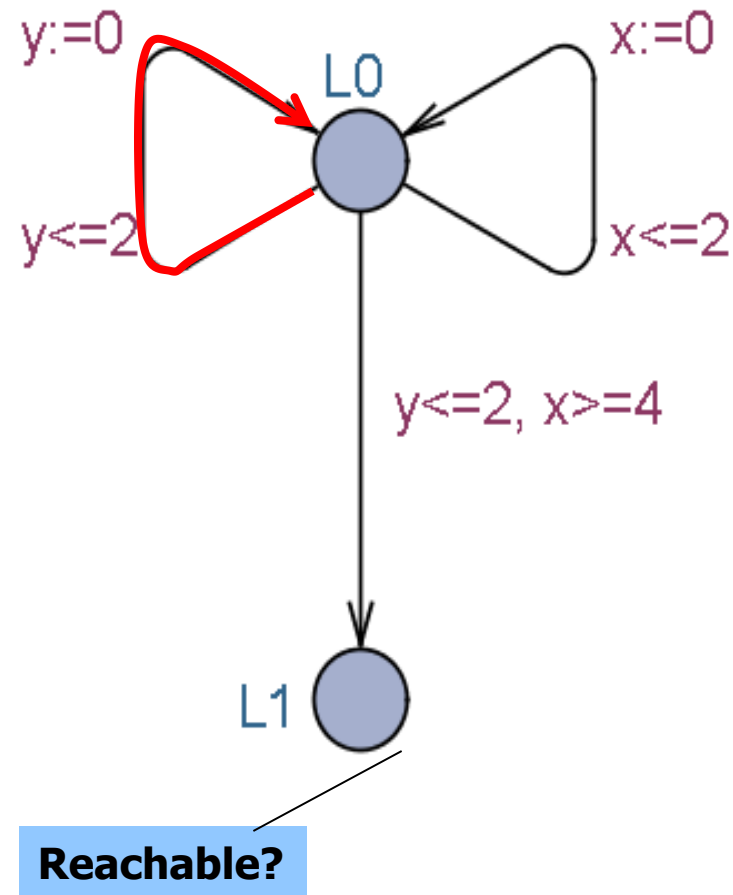


SYMBOLIC EXPLORATION

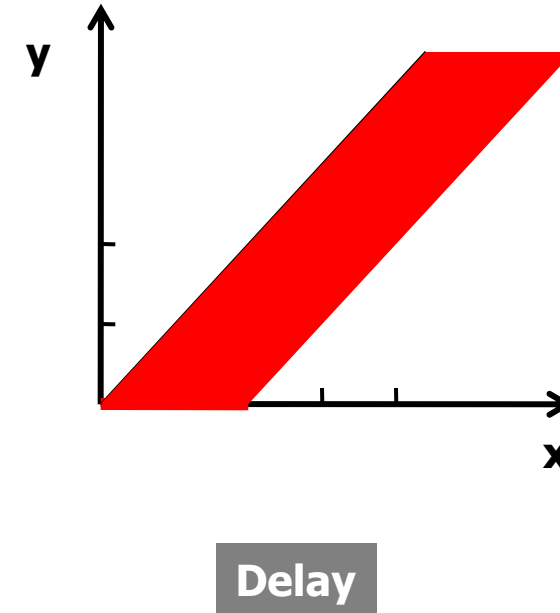
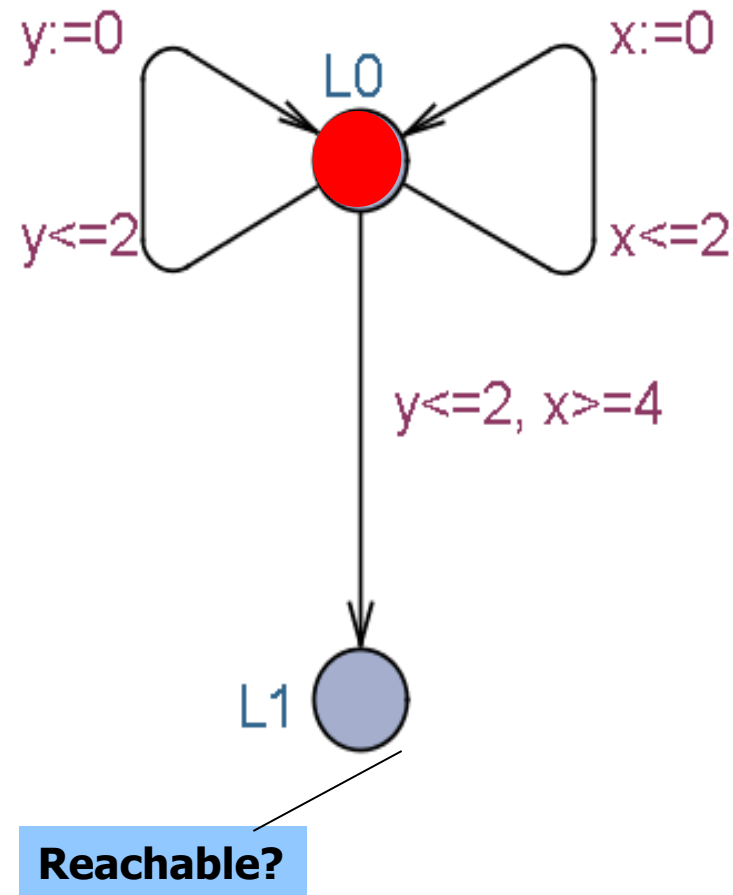


Left

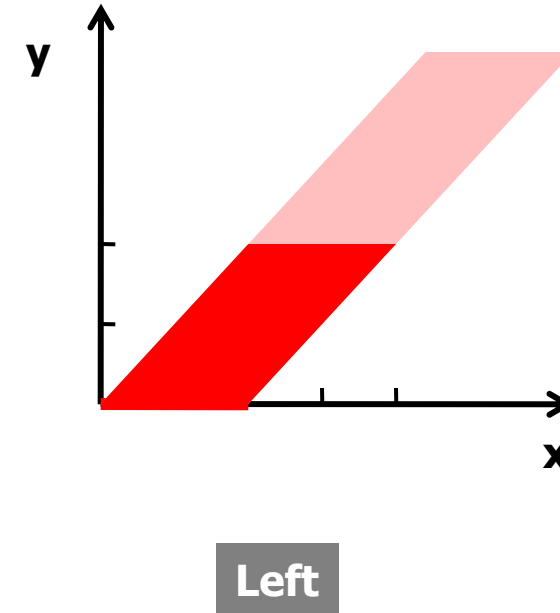
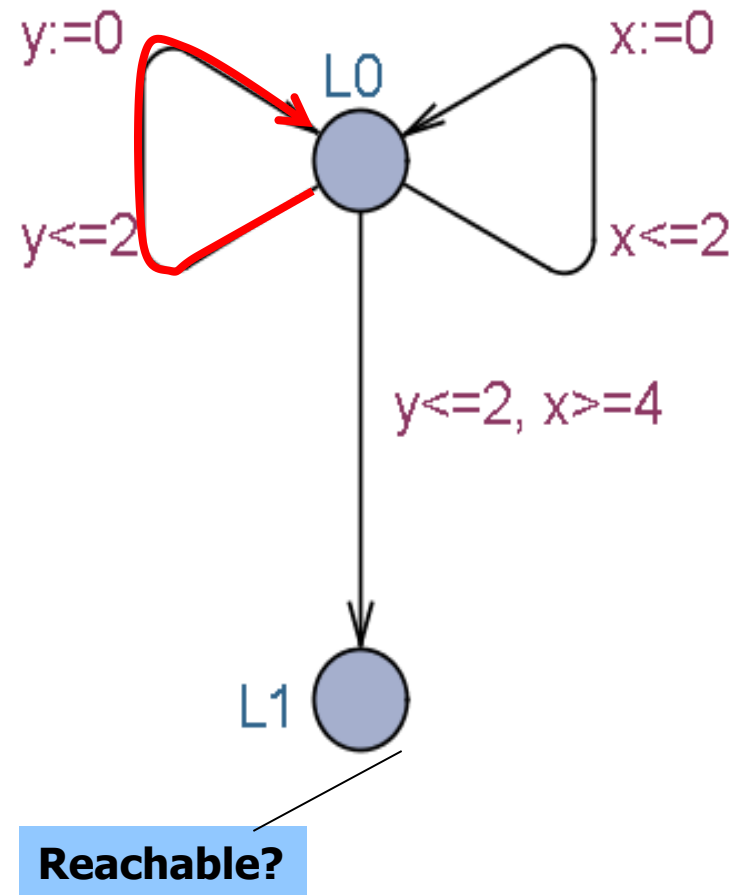
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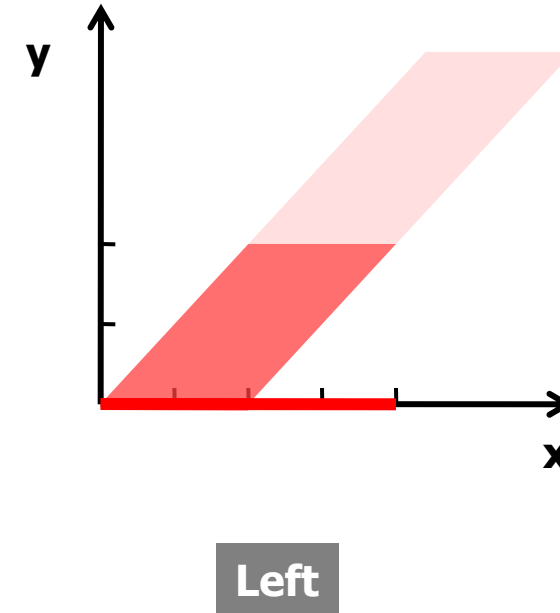
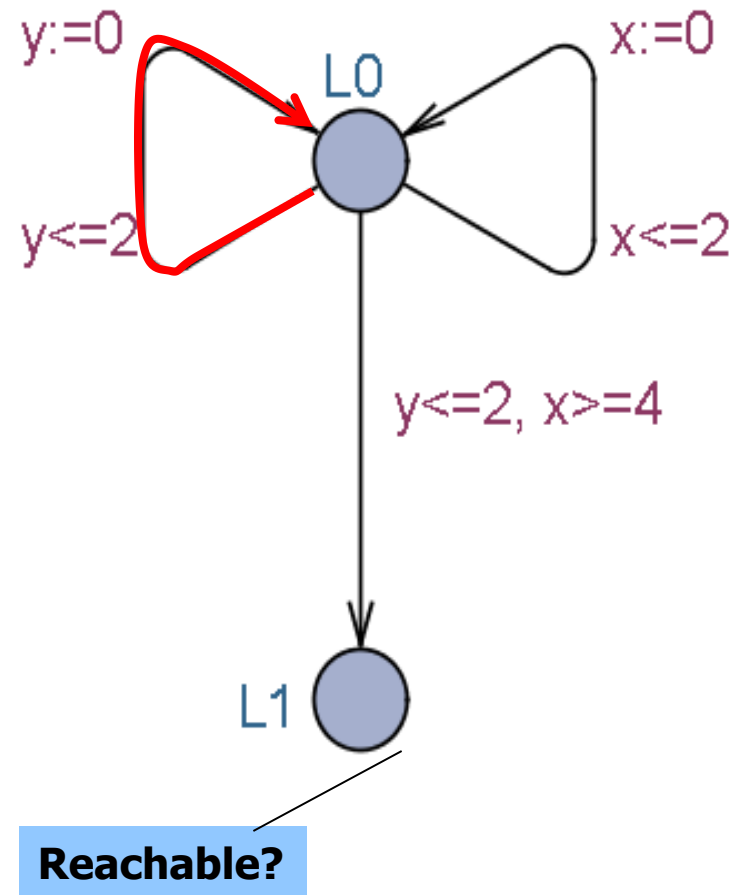
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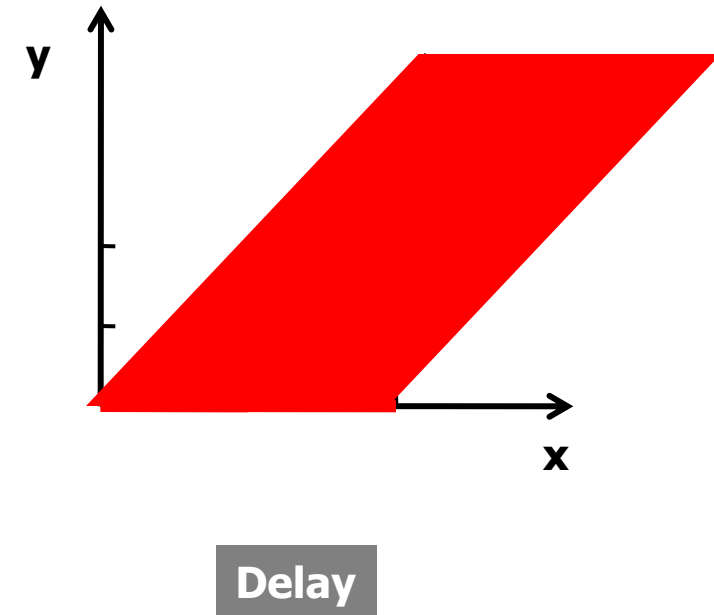
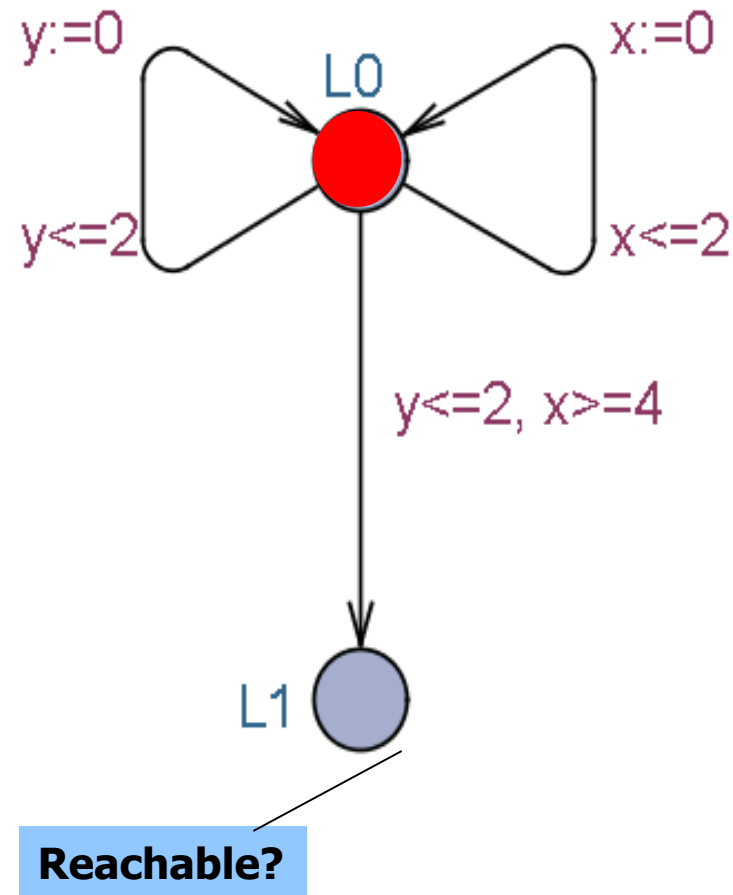
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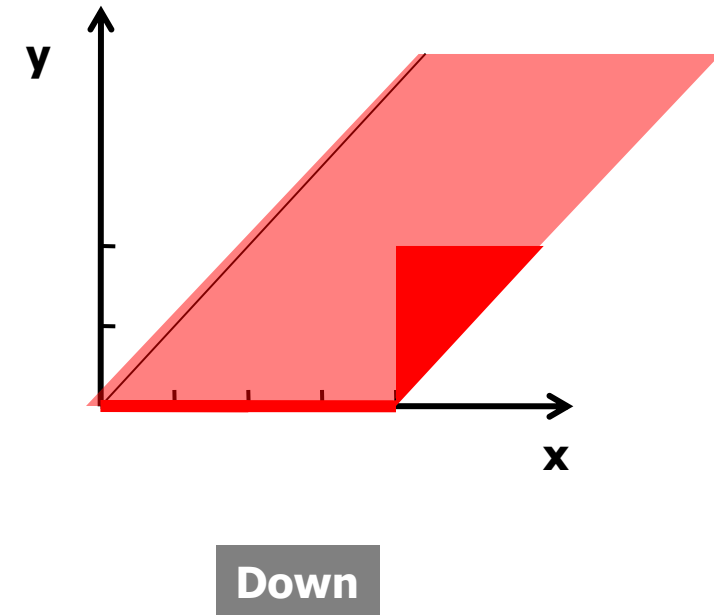
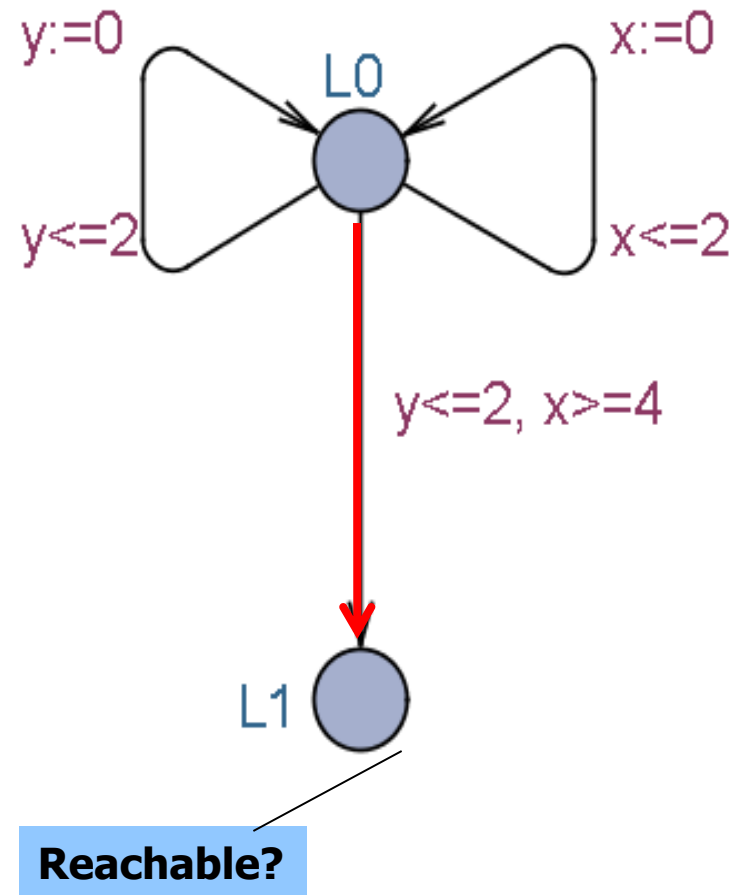
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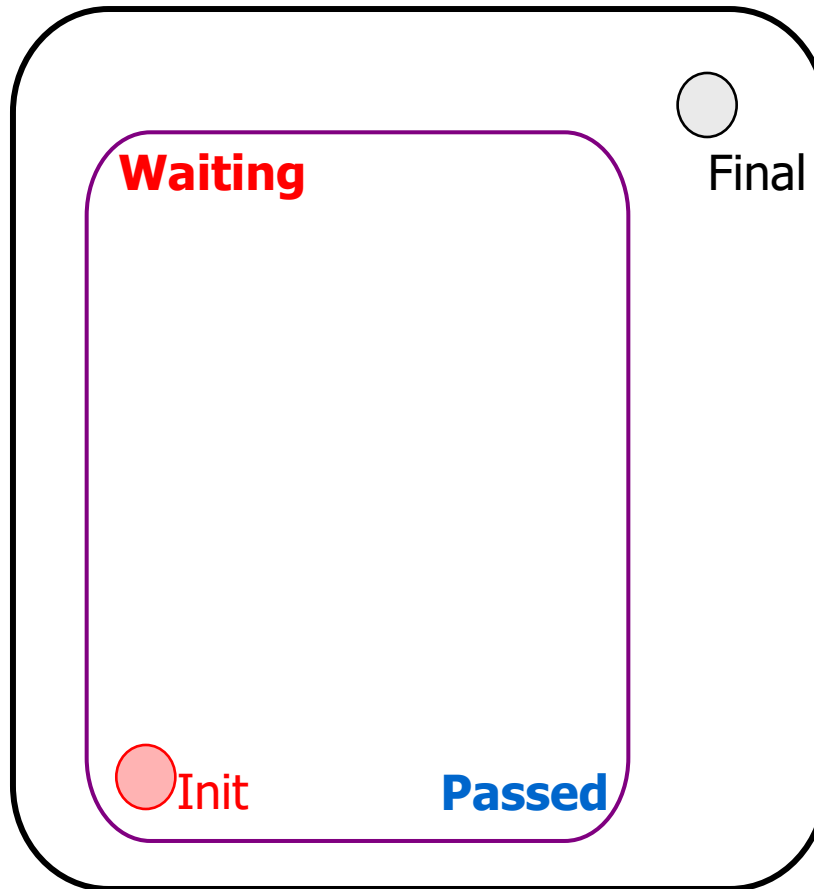


DEMO

Search order,
Clock constraints in simulator
Diagnostic trace

FORWARD REACHABILITY ALGORITHM

Init -> **Final** ?



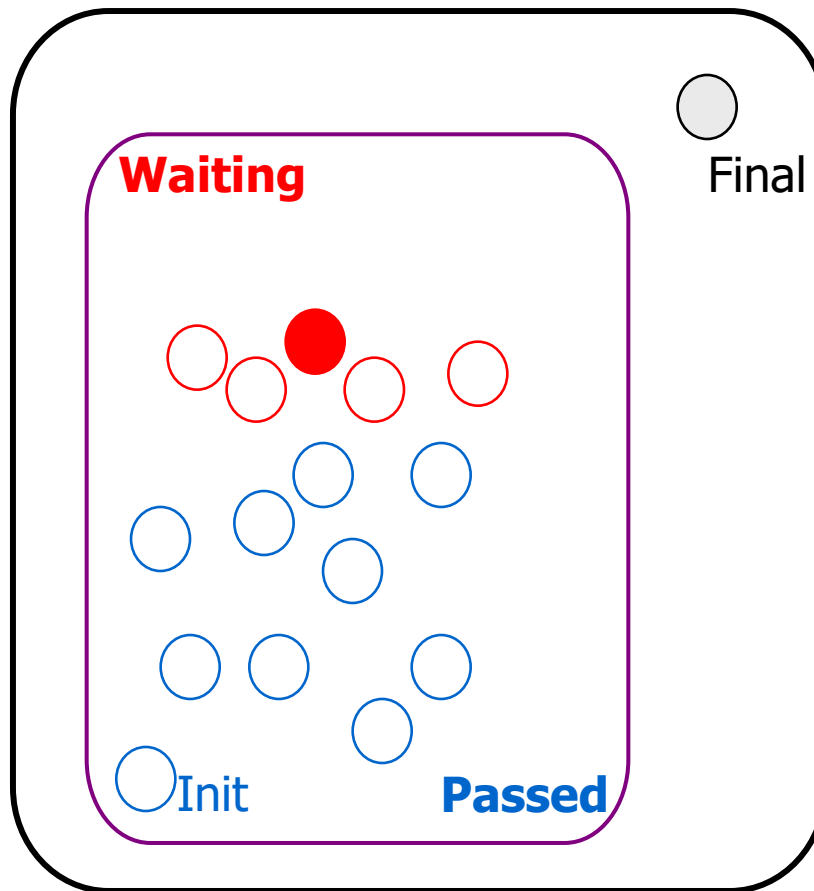
INITIAL **Passed** := \emptyset ;
Waiting := $\{(n_0, Z_0)\}$

REPEAT

UNTIL **Waiting** = \emptyset
return false

FORWARD REACHABILITY ALGORITHM

Init -> **Final** ?



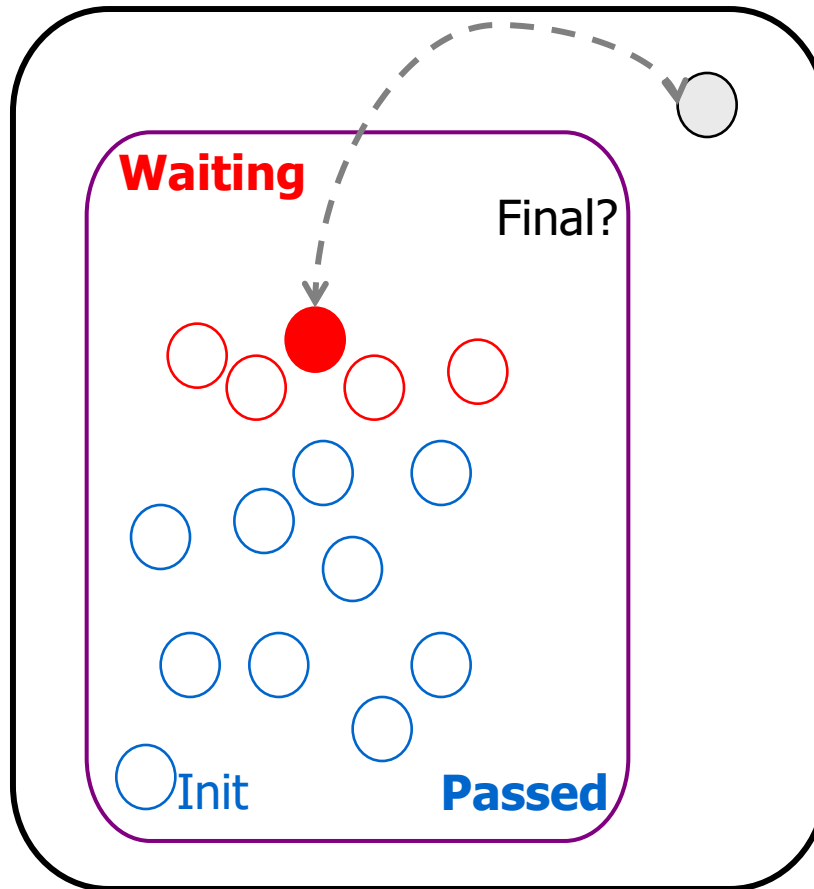
INITIAL **Passed** := \emptyset ;
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REPEAT
pick **(n,Z)** in **Waiting**

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FORWARD REACHABILITY ALGORITHM

Init -> **Final** ?



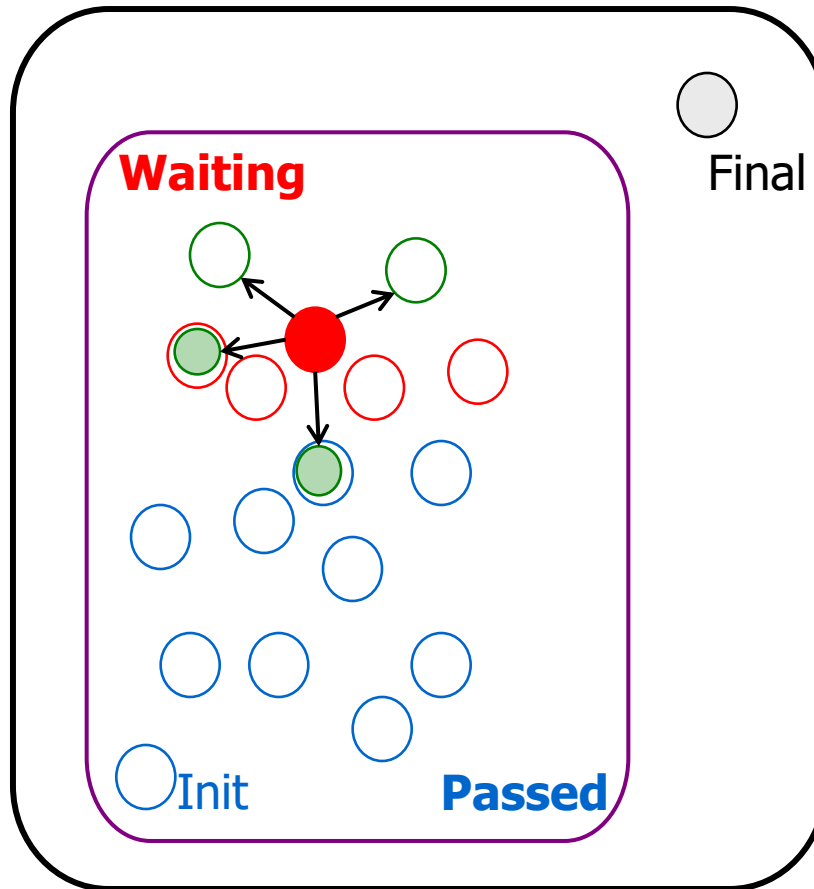
INITIAL **Passed** := \emptyset ;
Waiting := $\{(n_0, Z_0)\}$

REPEAT
 pick **(n,Z)** in **Waiting**
 if $(n,Z) = \text{Final}$ **return true**

UNTIL **Waiting** = \emptyset
return false

FORWARD REACHABILITY ALGORITHM

Init -> **Final** ?



INITIAL **Passed** := \emptyset ;
Waiting := $\{(n_0, Z_0)\}$

REPEAT

pick (n, Z) in **Waiting**

if $(n, Z) = \text{Final}$ **return true**

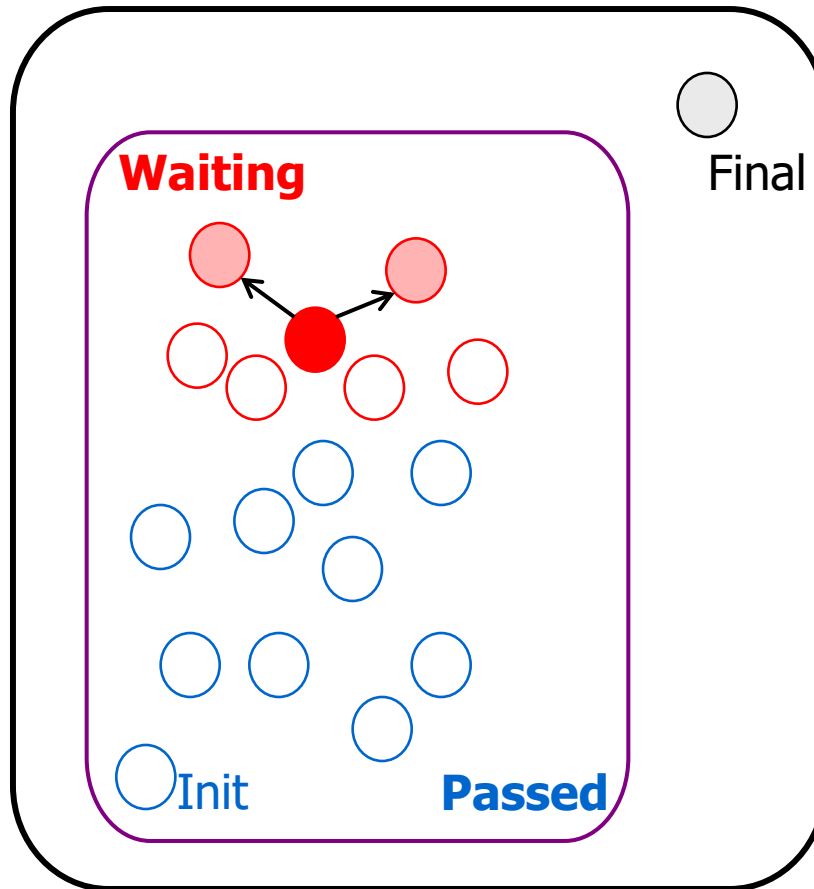
for all $(n, Z) \rightarrow (n', Z')$:

if for some (n', Z'') $Z' \subseteq Z''$ **continue**

UNTIL **Waiting** = \emptyset
return false

FORWARD REACHABILITY ALGORITHM

Init -> **Final** ?



INITIAL **Passed** := \emptyset ;
Waiting := $\{(n_0, Z_0)\}$

REPEAT

pick **(n,Z)** in **Waiting**

if $(n,Z) = \text{Final}$ **return true**

for all $(n,Z) \rightarrow (n',Z')$:

if for some (n',Z'') $Z' \subseteq Z''$ **continue**

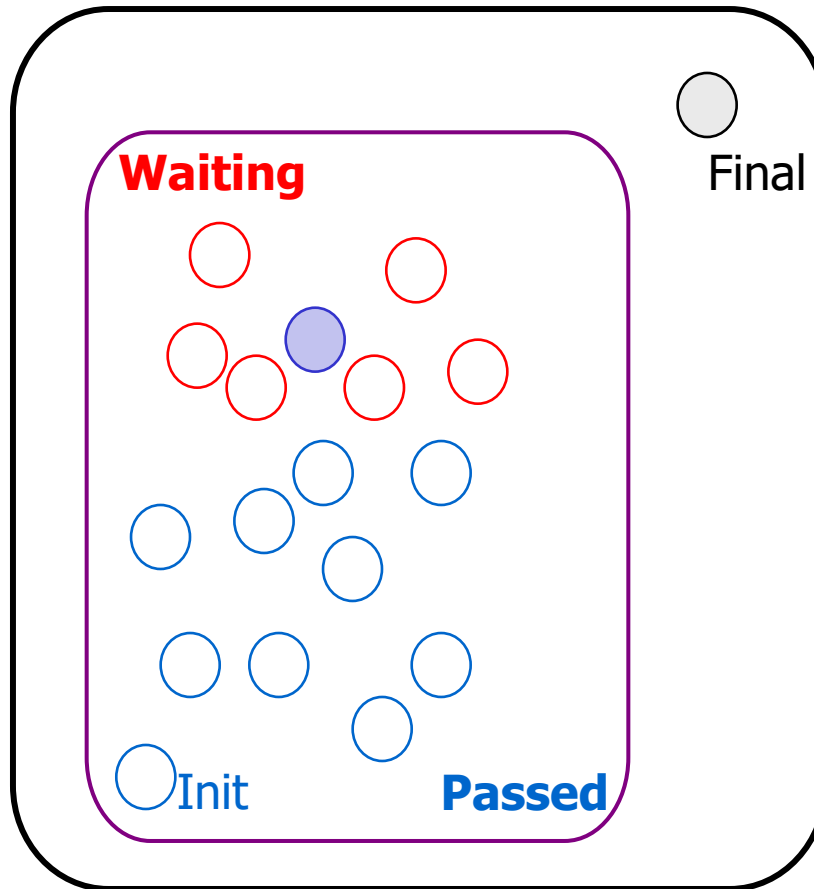
else add (n',Z') to **Waiting**

UNTIL **Waiting** = \emptyset

return false

FORWARD REACHABILITY ALGORITHM

Init -> Final ?



INITIAL **Passed** := \emptyset ;
Waiting := $\{(n_0, Z_0)\}$

REPEAT

pick **(n,Z)** in **Waiting**

if $(n,Z) = \text{Final}$ **return true**

for all $(n,Z) \rightarrow (n',Z')$:

if for some (n',Z'') $Z' \subseteq Z''$ **continue**

else add (n',Z') to **Waiting**

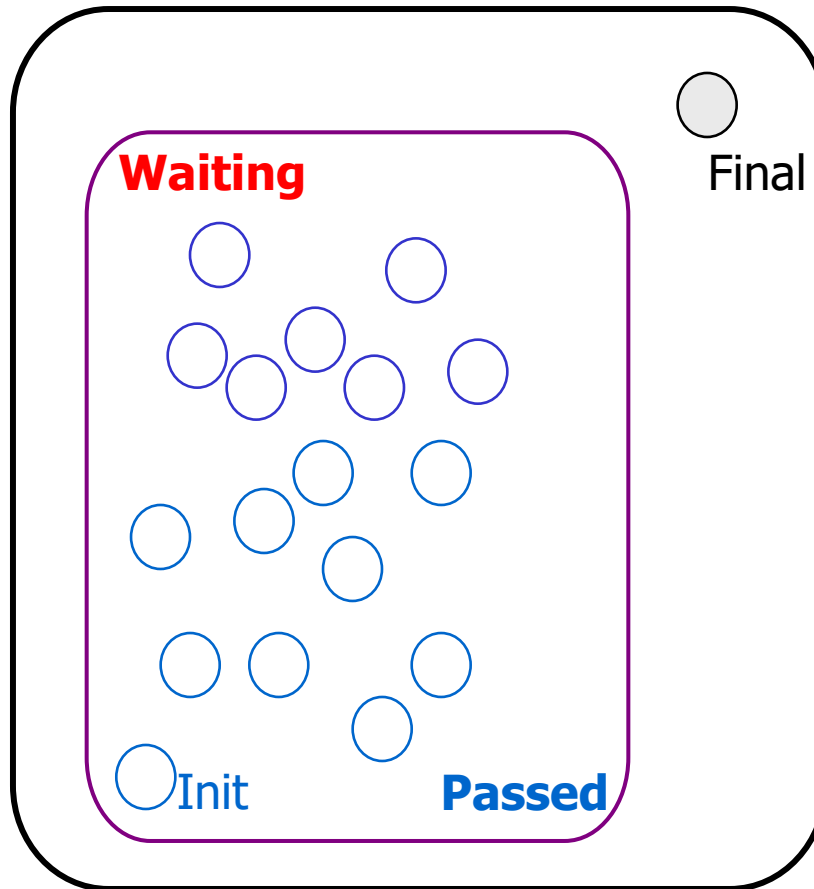
move (n,Z) to **Passed**

UNTIL **Waiting** = \emptyset

return false

FORWARD REACHABILITY ALGORITHM

Init -> Final ?



INITIAL **Passed** := \emptyset ;
Waiting := $\{(n_0, Z_0)\}$

REPEAT

pick **(n,Z)** in **Waiting**

if $(n,Z) = \text{Final}$ **return true**

for all $(n,Z) \rightarrow (n',Z')$:

if for some (n',Z'') $Z' \subseteq Z''$ **continue**

else add (n',Z') to **Waiting**

move (n,Z) to **Passed**

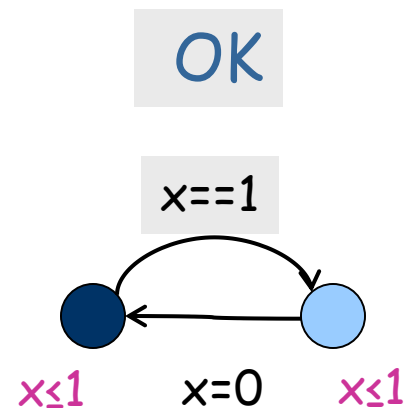
UNTIL **Waiting** = \emptyset

return false

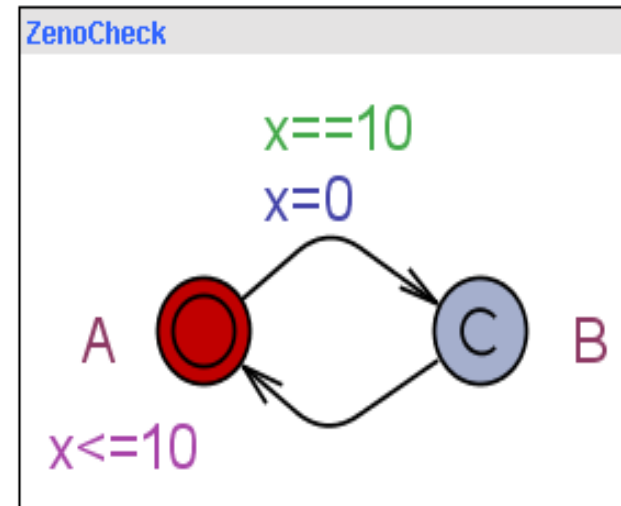
ZENONESS

- **Problem:** UPPAAL does not check for zenoness directly.
 - A model has “zeno” behavior if it can take an **infinite amount of actions in finite time**.
 - That is usually not a desirable behavior in practice.
 - Zeno models may wrongly conclude that some properties hold though they logically should not.
 - Rarely taken into account.
- **Solution:** Add an observer automata and check for non-zenoness, i.e., that time will always pass.

ZENONESS



Detect by
• adding the
observer:



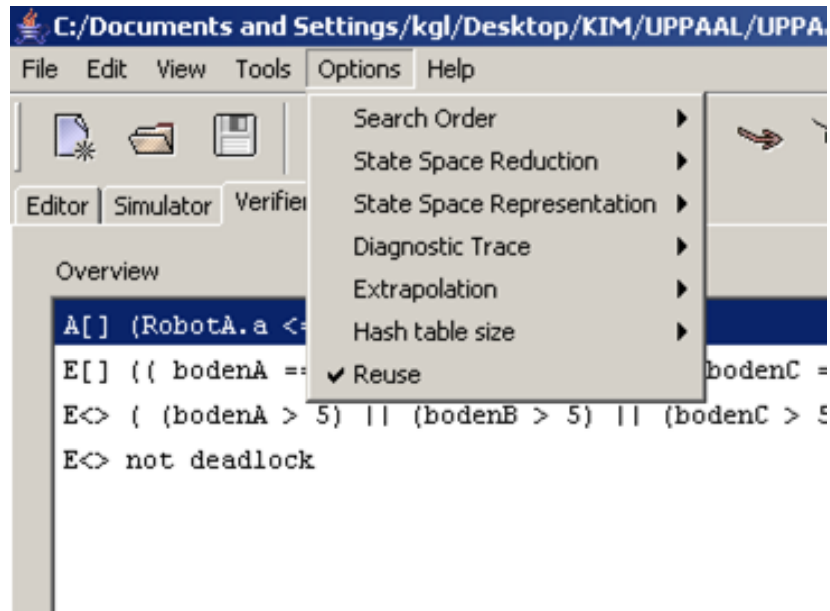
Constant (10) can be anything (>0), but choose it well w.r.t. your model for efficiency. Clocks 'x' are local.

• and check the property

ZenoCheck.A --> ZenoCheck.B

VERIFICATION OPTIONS

VERIFICATION OPTIONS



Search Order

Depth First

Breadth First

State Space Reduction

None

Conservative

Aggressive

State Space Representation

DBM

Compact Form

Under Approximation

Over Approximation

Diagnostic Trace

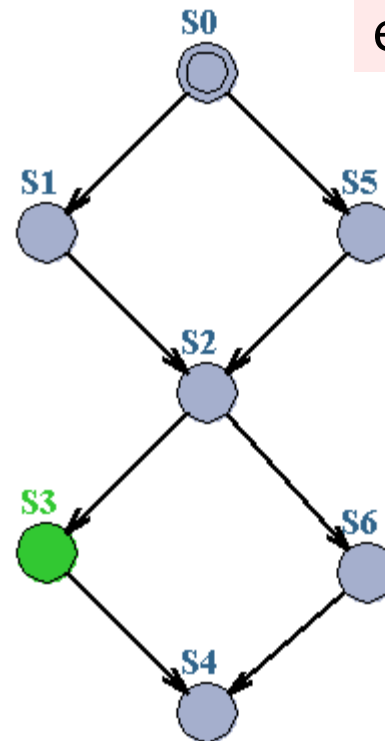
Some

Shortest

Fastest

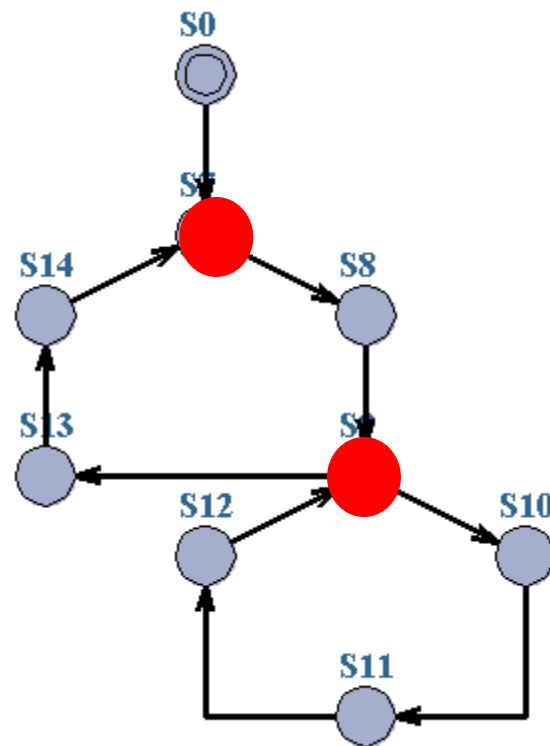
STATE SPACE REDUCTION

However,
Passed list useful for
efficiency



No Cycles: **Passed** list not needed for *termination*

STATE SPACE REDUCTION



Cycles:

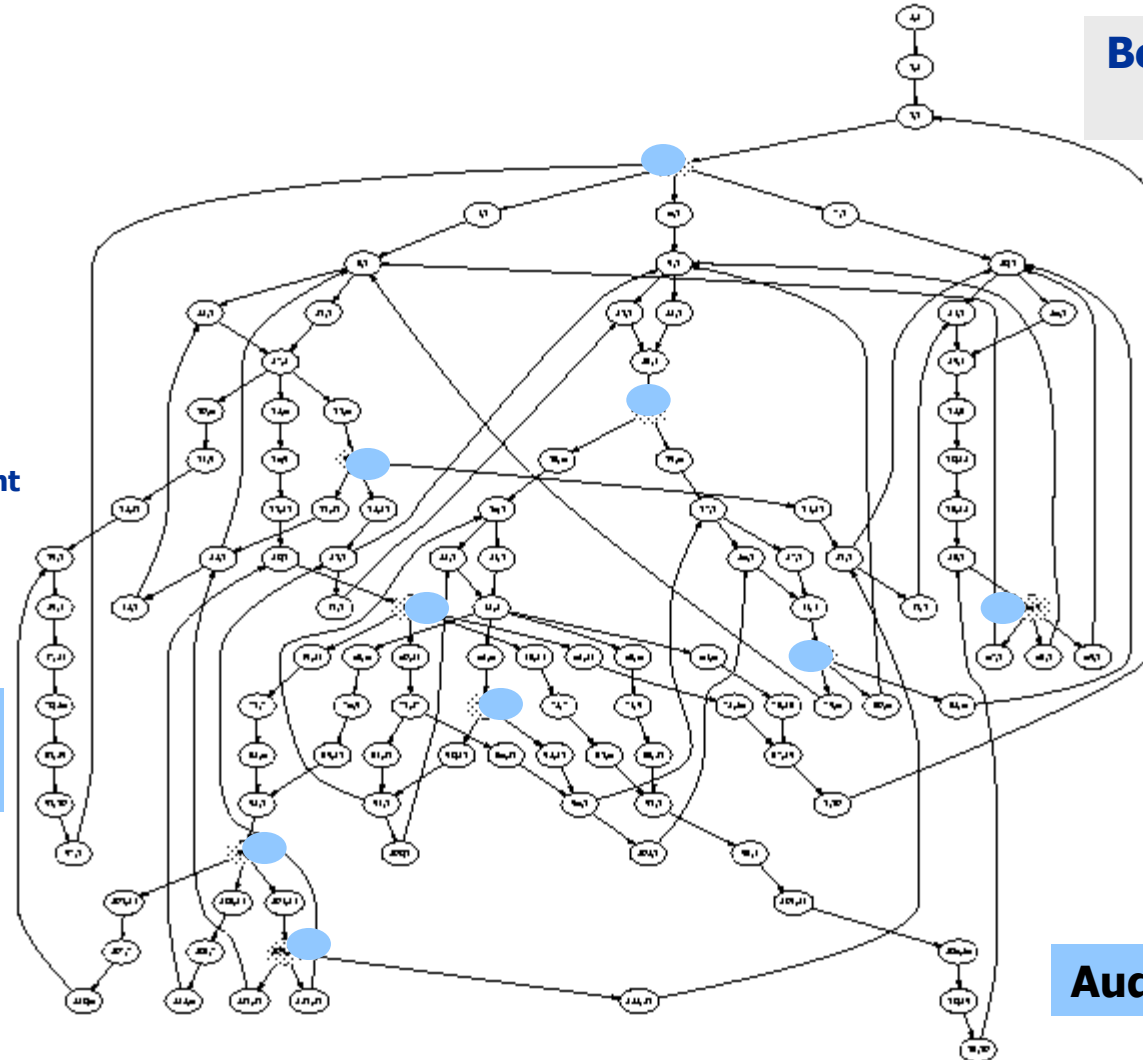
Only symbolic states
involving loop-entry points
need to be saved on **Passed** list

TO STORE OR NOT TO STORE

Behrmann, Larsen,
Pelanek 2003

117 states_{total}
!
81 states_{entrypoint}
!
9 states

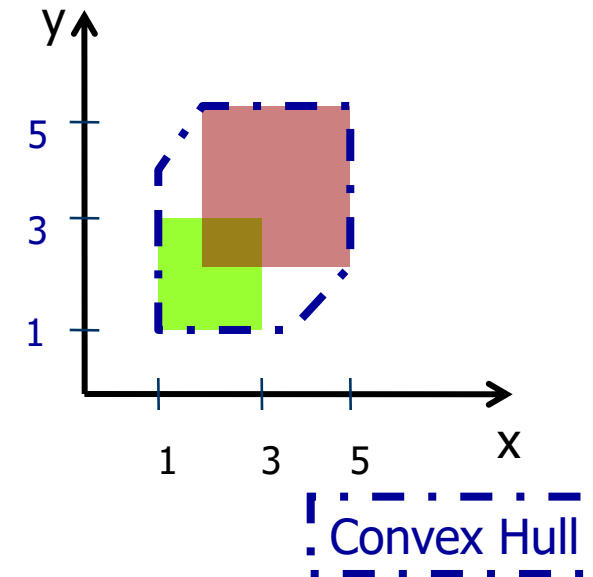
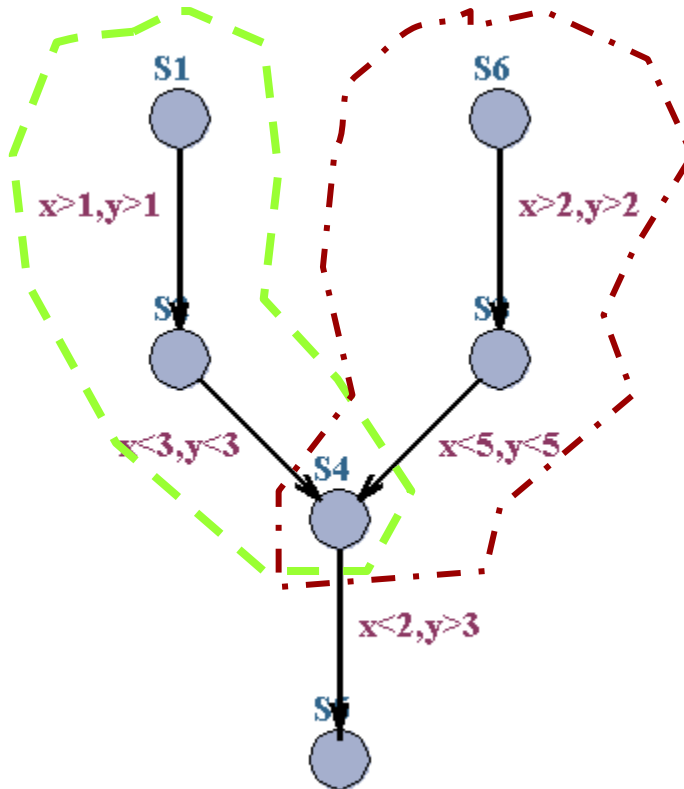
Time OH
less than 10%



Audio Protocol

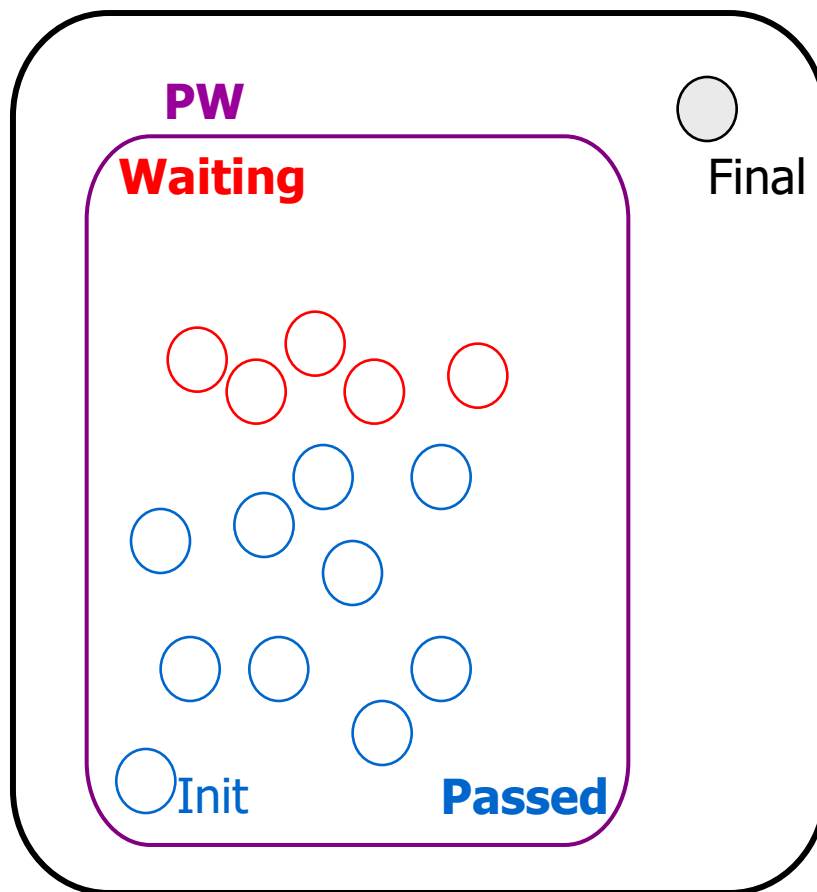
OVER-APPROXIMATION

TACAS04: An **EXACT** method performing as well as Convex Hull has been developed based on abstractions taking max constants into account.



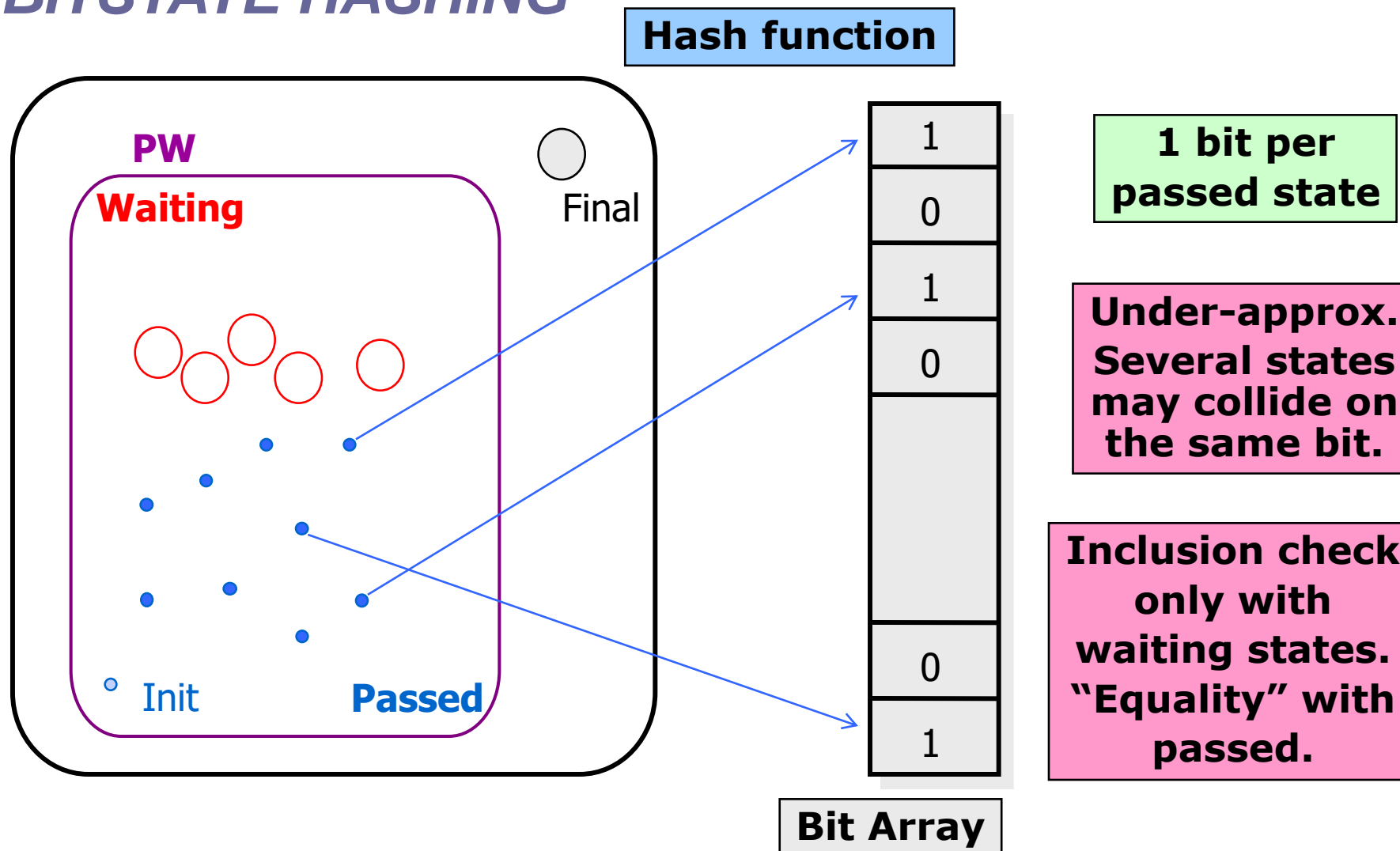
UNDER-APPROXIMATION

BITSTATE HASHING



UNDER-APPROXIMATION

BITSTATE HASHING



MODELLING PATTERNS

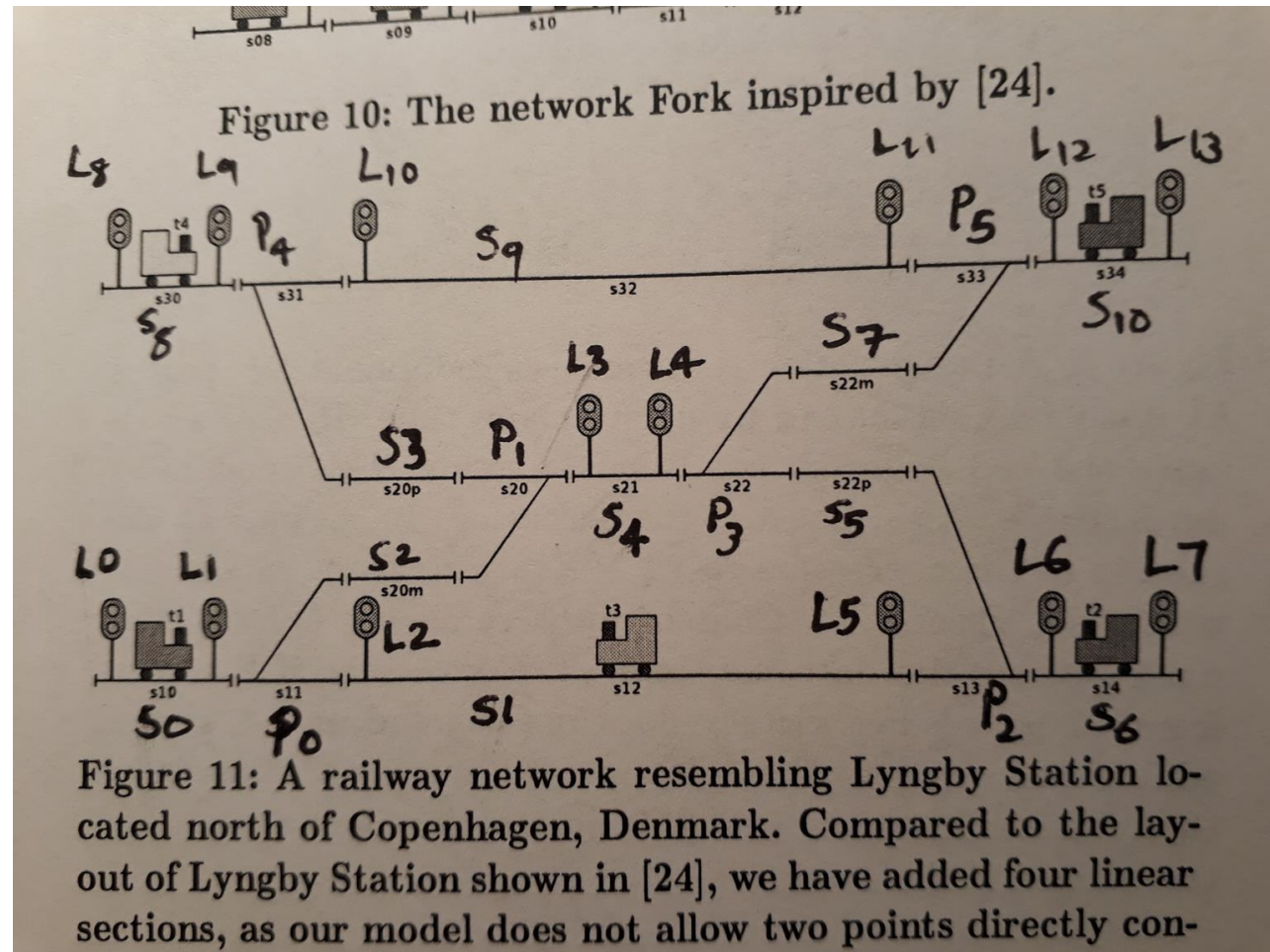
VARIABLE REDUCTION

- Reduce size of state space by explicitly resetting variables when they are not used!
- Automatically performed for clock variables (active clock reduction)

```
// Remove the front element of the queue  
void dequeue()  
{  
    int i = 0;  
    len -= 1;  
    while (i < len)  
    {  
        list[i] = list[i + 1];  
        i++;  
    }  
    list[i] = 0;  
}
```

VARIABLE REDUCTION

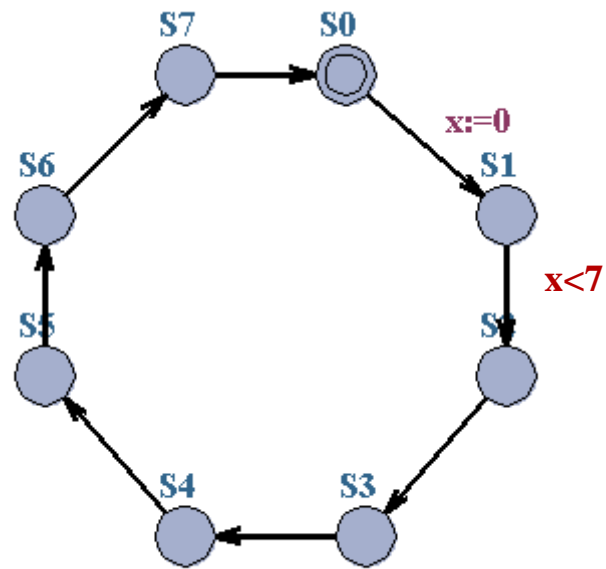
■ Railway controller



VARIABLE REDUCTION

```
section_Id go(int tId){
    int pos=position[tId];
    bool dir=direction[tId];
    if(pos==0 and dir==0) {crash=true; return pos;}
    if(pos==0 and dir==1) {if(config_Of_Points[0]==0){
        if(occupied[1]==0){
            occupied[1]=1;
            occupied[0]=0;
            return 1;
        } else {
            crash = true;
            return pos;}
        } else {
            if(occupied[2]==0){
                occupied[2]=1;
                occupied[0]=0;
                return 2;
            } else {
                crash = true;
                return pos;}
            }
        }
    }
    if(pos==1 and dir==0) {if(occupied[0]==0){
        occupied[0]=1;
        occupied[1]=0;
        return 0;
    } else {
```

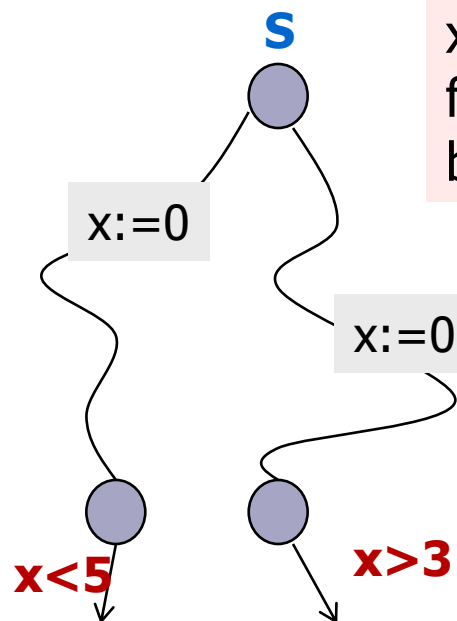
CLOCK REDUCTION (AUTOMATIC)



x is only *active* in location **S1**

Definition

x is *inactive* at **S** if on all path from **S**, x is always reset before being tested.



THINGS YOU SHOULD KNOW BY THE END OF TODAY

- ≡ What is a Timed Automata?
- ≡ How is time treated in a finite way?
- ≡ Why do we need both committed and urgent locations?
- ≡ How can I check if a model can reach a certain state?

PART 2: OTHER UPPAAL BASED TOOLS

AGENDA

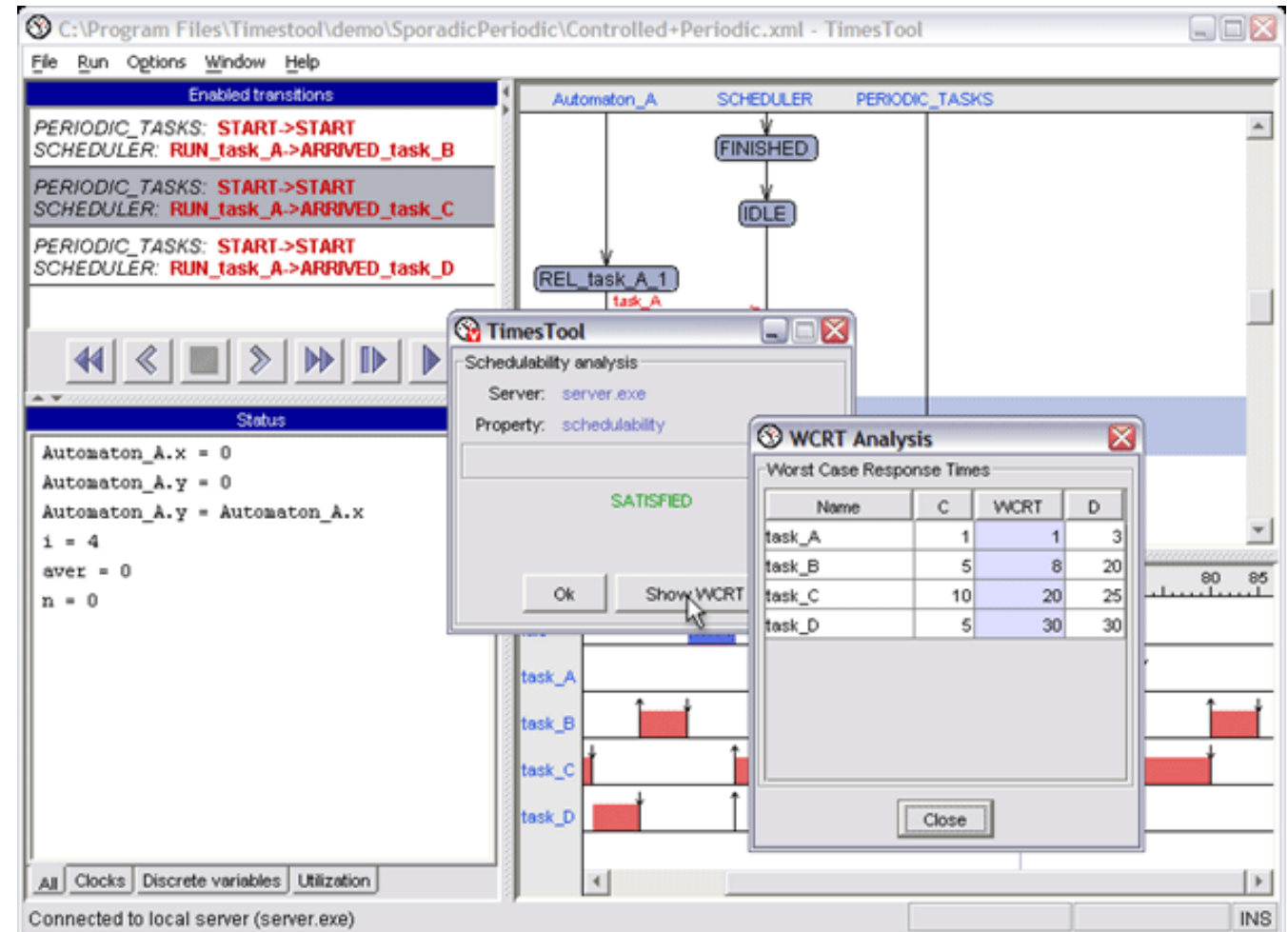
- TIMES
- Uppaal TIGA
- Uppaal CORA
- Uppaal PORT
- Uppaal cover
- Uppaal PRO
- Uppaal SMC (a.k.a. Uppaal 4.1.9)
- Uppaal Stratego
- Uppaal TRON
- ECDAR/Jecdar/Hecdar

WHY SO MANY TOOLS?

- ≡ This is an academic tool
- ≡ New experiments require new tools
- ≡ **No publications in merging tools**
- ≡ No funding to hire someone for tool maintenance
- ≡ Some models may look similar, but cannot be combined

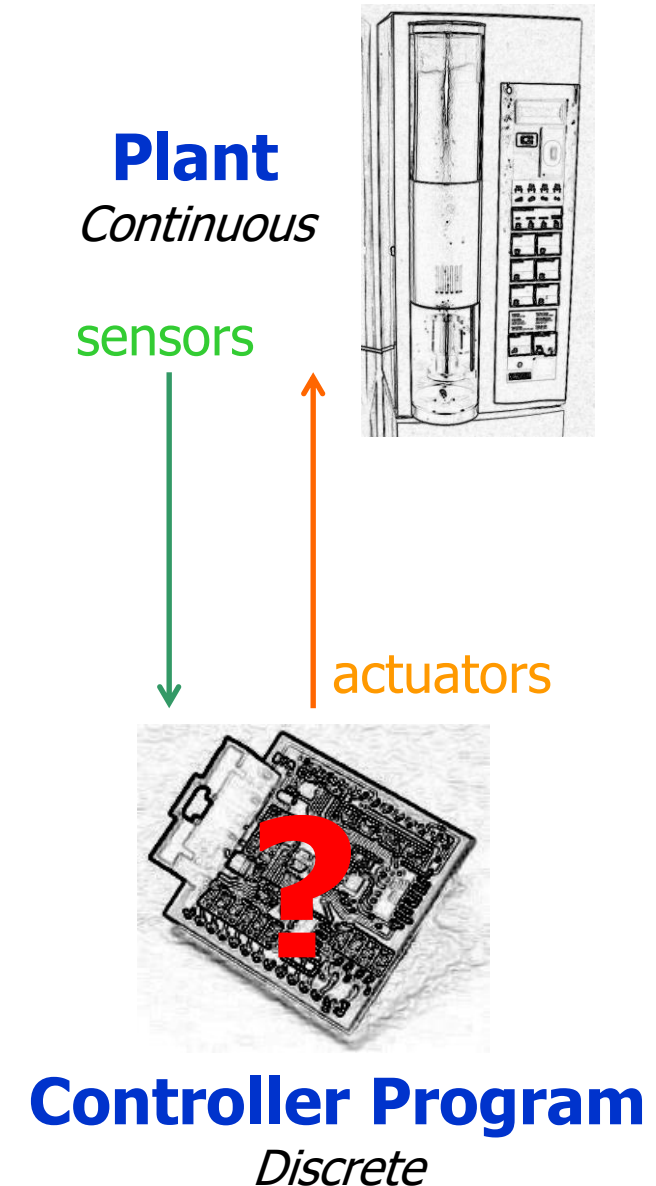
TIMES

- ≡ 2002
- ≡ *Disclaimer: I have never used this tool*
- ≡ Same underlying model checking engine
- ≡ Very different modeling possibilities
- ≡ Targeted at
 - ≡ Schedulability analysis
 - ≡ Generating optimal schedules



UPPAAL TIGA

- ≡ TIGA = Timed Games
 - ≡ Two player games
 - ≡ Controllable and uncontrollable actions
- ≡ Controller synthesis:
 - ≡ Model the environment + what a controller can do.
 - ≡ Generate the controller so that controller satisfies φ !
 - ≡ Generate the right code automatically.
- ≡ 2-player timed game:
 - environment moves vs. controller moves.
 - Timed Game Automata.

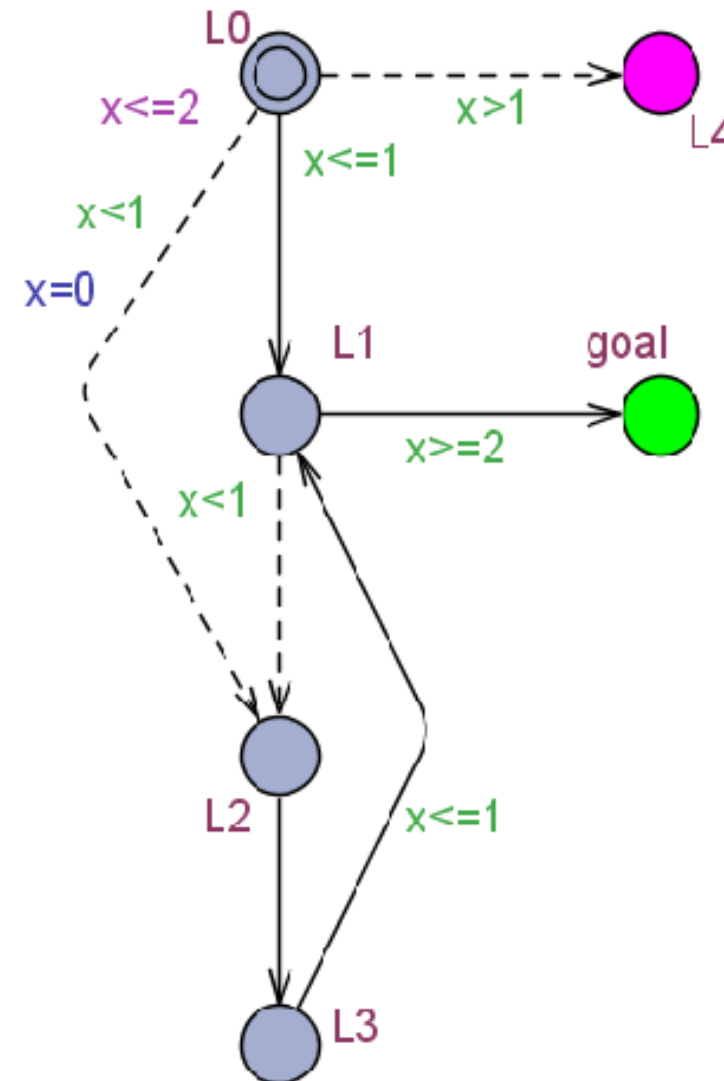


CONTROLLER SYNTHESIS/TGA

- ≡ Given
 - ≡ System moves S ,
 - ≡ Controller moves C ,
 - ≡ and a property φ ,
 - ≡ find
 - ≡ a strategy Sc s.t. $Sc||S$ satisfies φ ,
 - ≡ or prove there is no such strategy.
-
- ≡ The controller continuously observes the system (all delays & moves are observable).
 - ≡ The controller can
 - ≡ wait (delay action),
 - ≡ take a controllable move, or
 - ≡ prevent delay by taking a controllable move

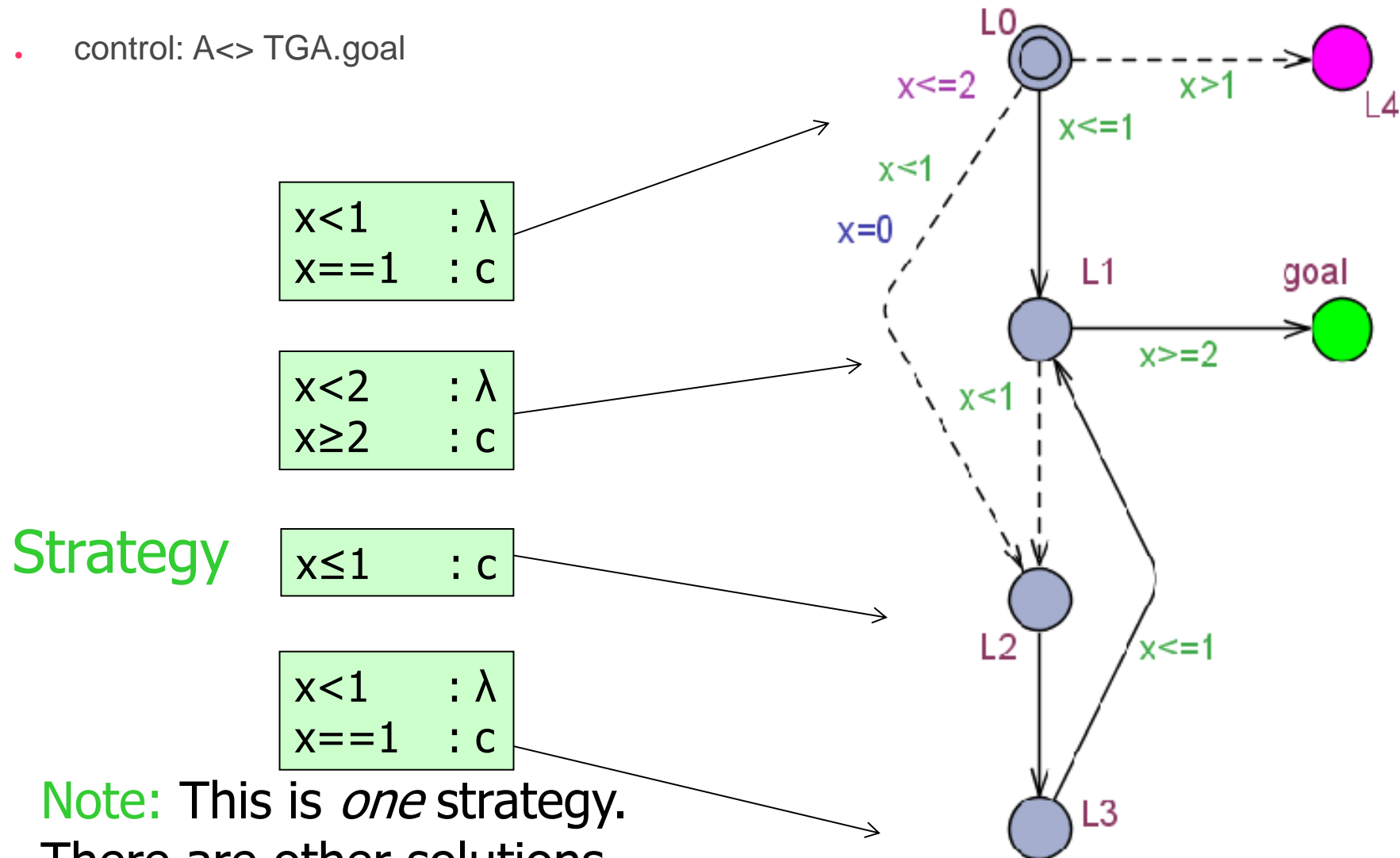
TIMED GAME AUTOMATA

- ≡ Timed automata with controllable and uncontrollable transitions.
- ≡ Reachability & safety games.
 - ≡ control: $A \leftrightarrow \text{TGA.goal}$
 - ≡ control: $A[]$ not TGA.L4
- ≡ Memoryless strategy:
 - ≡ state \rightarrow action.



TGA – LET’S PLAY!

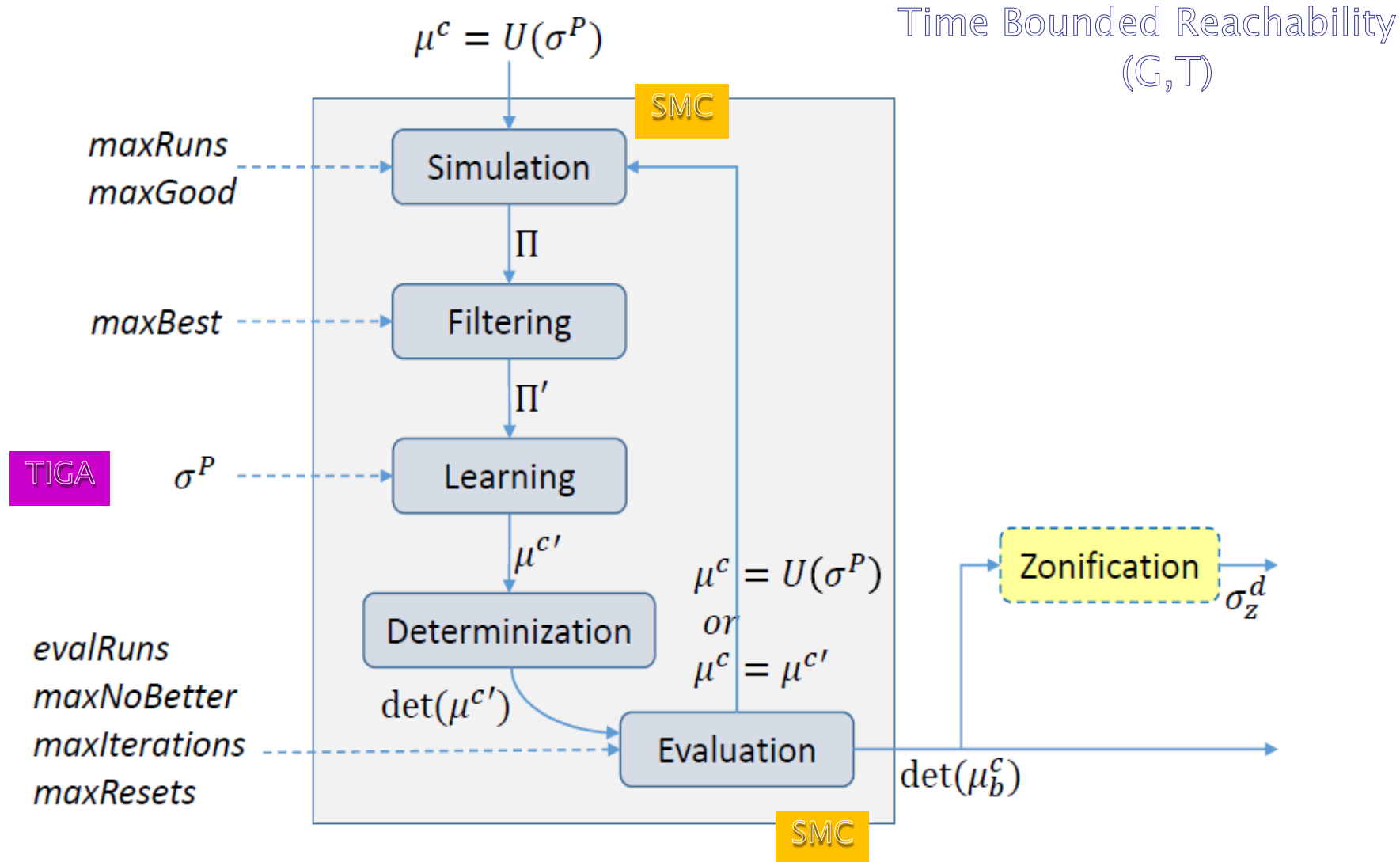
- control: $A \leftrightarrow \text{TGA.goal}$



Strategy

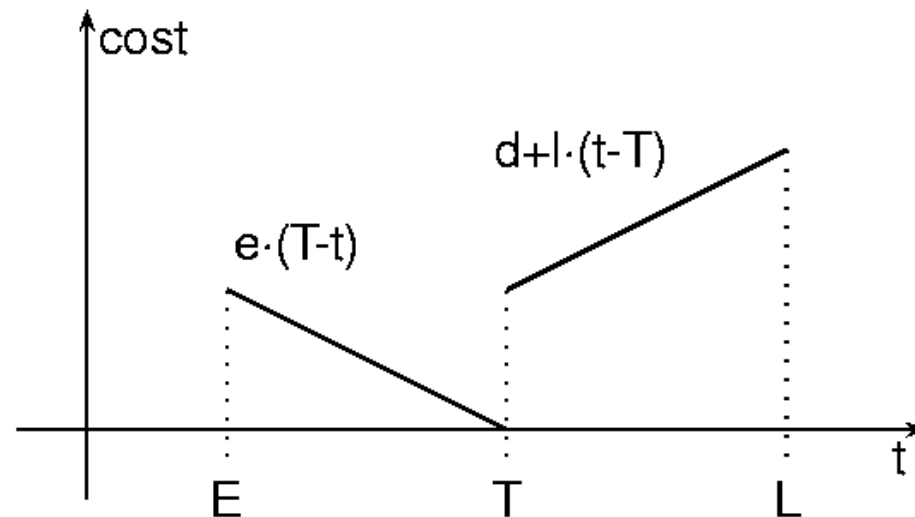
Note: This is *one* strategy.
There are other solutions.

Reinforcement Learning



UPPAAL CORA

- ≡ CORA = Cost Optimal Reachability Analysis
- ≡ UPPAAL for Planning and Scheduling
- ≡ Enables modeling LPTA
 - ≡ LPTA = Linearly priced timed automata
 - ≡ Can model e.g. energy consumption
 - ≡ Discrete costs on edges
 - ≡ Linear cost accumulating in locations



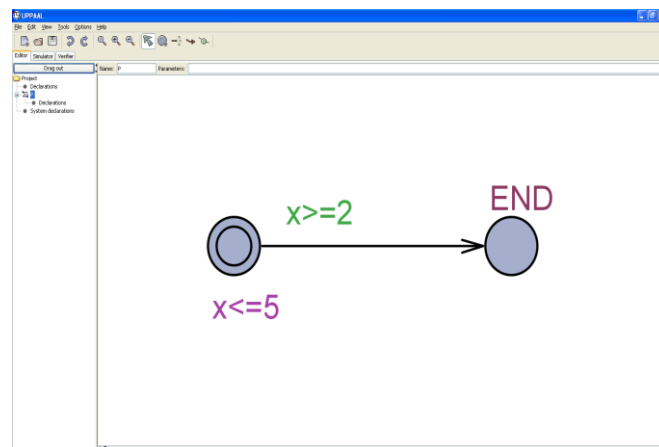
- E earliest landing time
- T target (cruise) landing time
- L latest landing time
- e early cost rate
- l late cost rate
- d late penalty

UPPAAL SMC

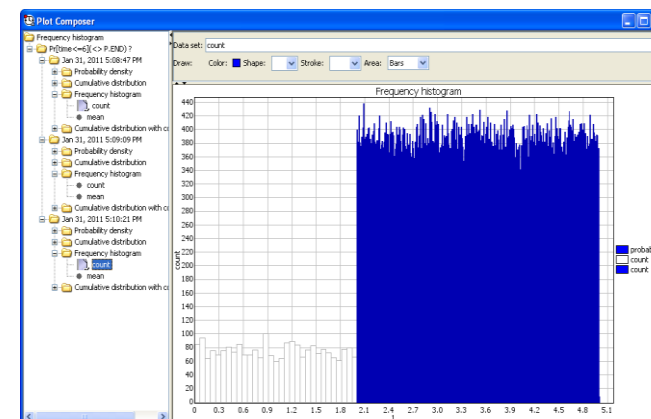
- ≡ Statistical model checking
- ≡ Now integrated in main UPPAAL
- ≡ This is really simulation
 - ≡ A LOT of simulation
 - ≡ With a calculated confidence level

- ≡ State space explosion not a (big) problem
- ≡ Evaluation of other approaches
- ≡ Very fast compared to testing

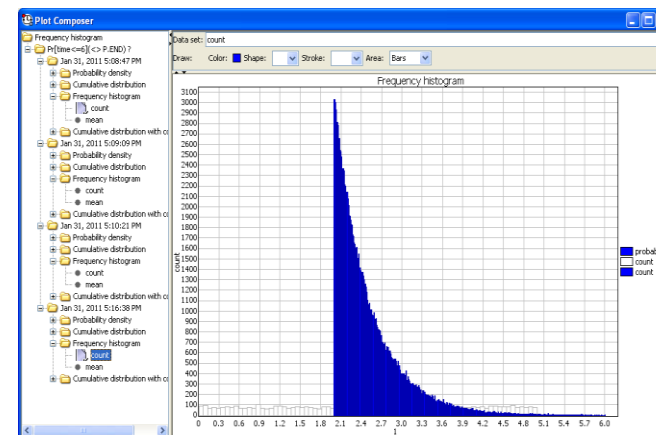
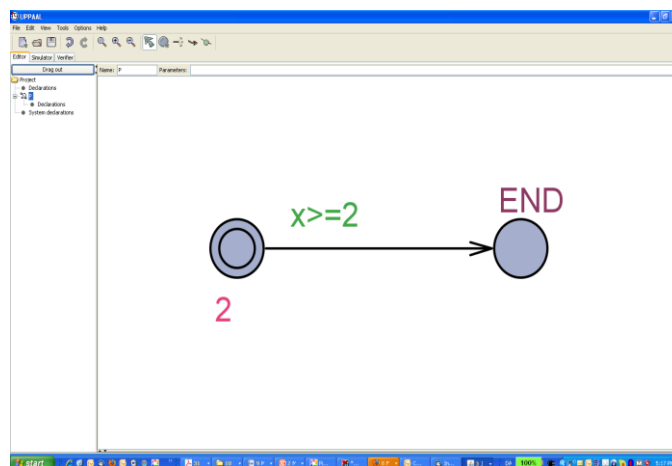
DELAY

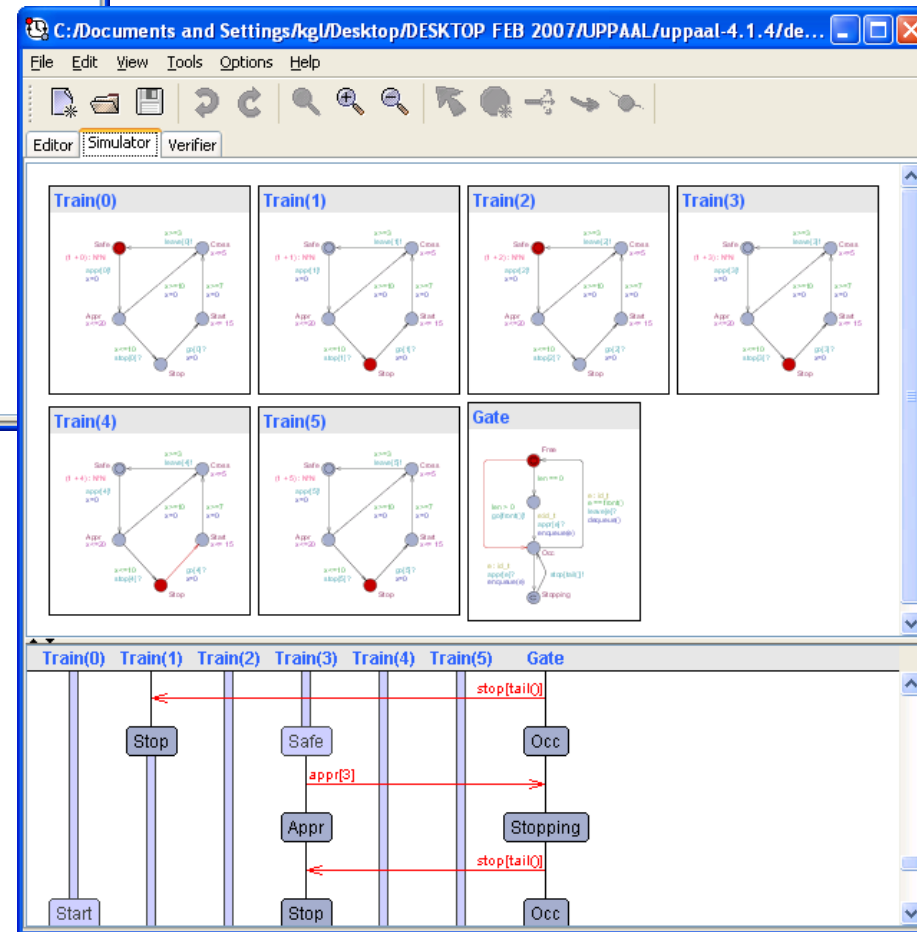
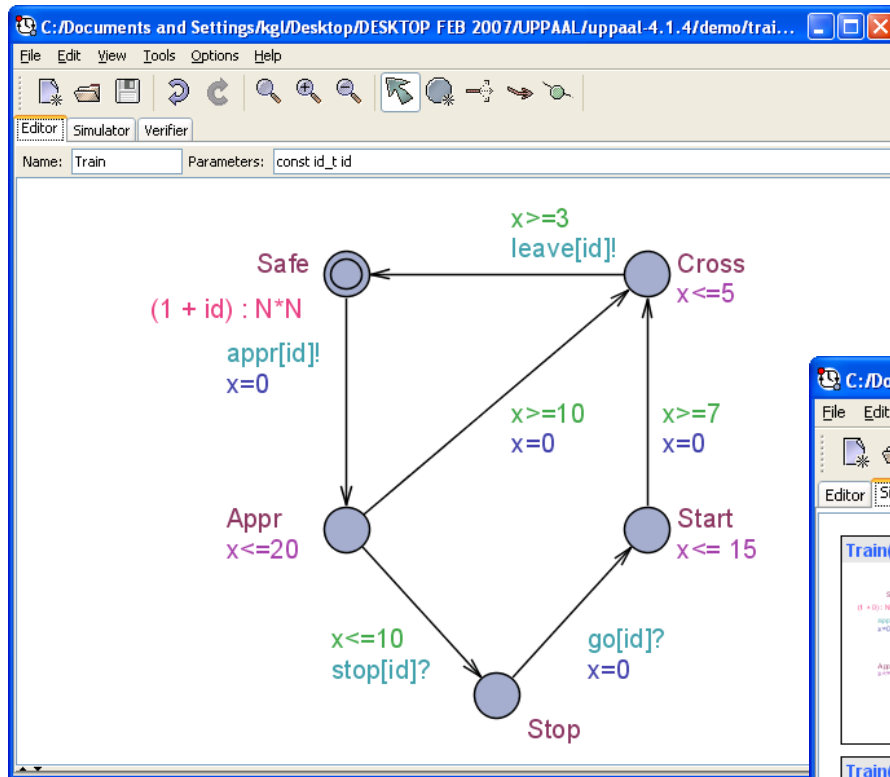


Uniform



Exponential (rate)

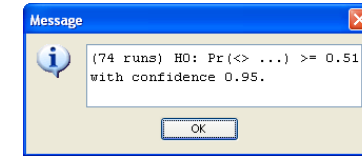




QUERIES

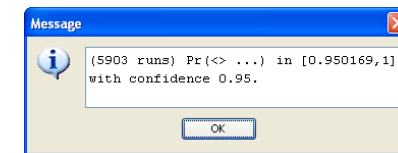
≡ Qualitative Check (Hypothesis Testing)

≡ $\text{Pr}[\text{time} \leq 500](\langle \rangle \text{Train}(0).\text{Cross}) \geq 0.5$



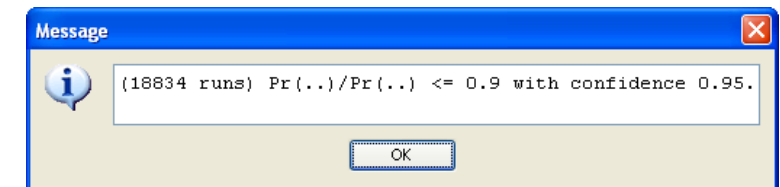
≡ Quantitative Check (Estimation)

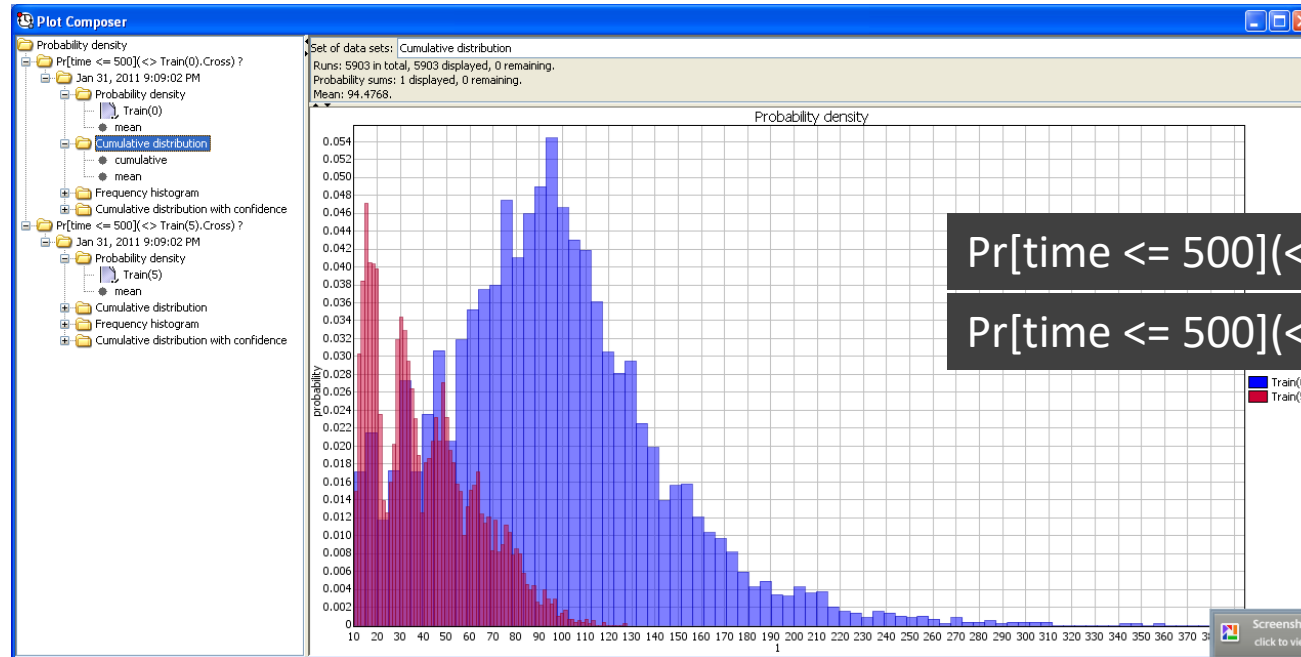
≡ $\text{Pr}[\text{time} \leq 500](\langle \rangle \text{Train}(5).\text{Cross}) ?$



≡ Comparison Test

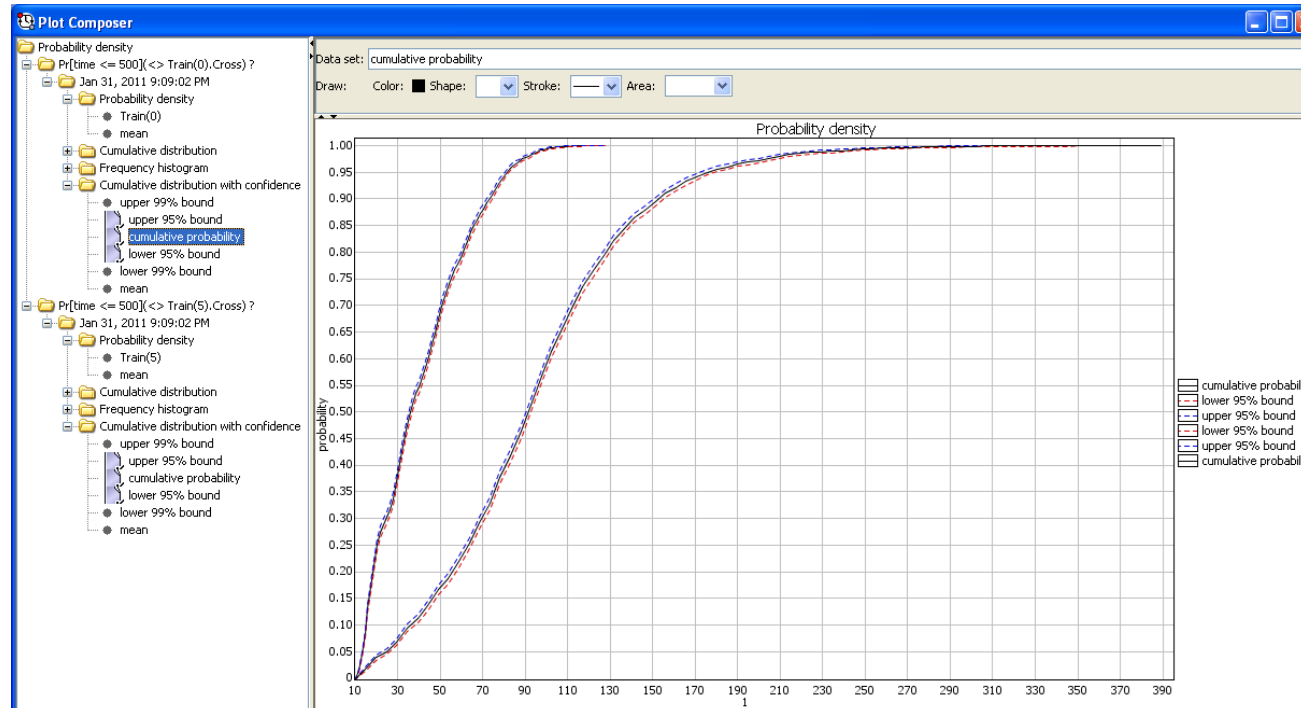
≡ $\text{Pr}[\text{time} \leq 500](\langle \rangle \text{Train}(5).\text{Cross}) \geq$
 $\text{Pr}[\text{time} \leq 500](\langle \rangle \text{Train}(0).\text{Cross})$



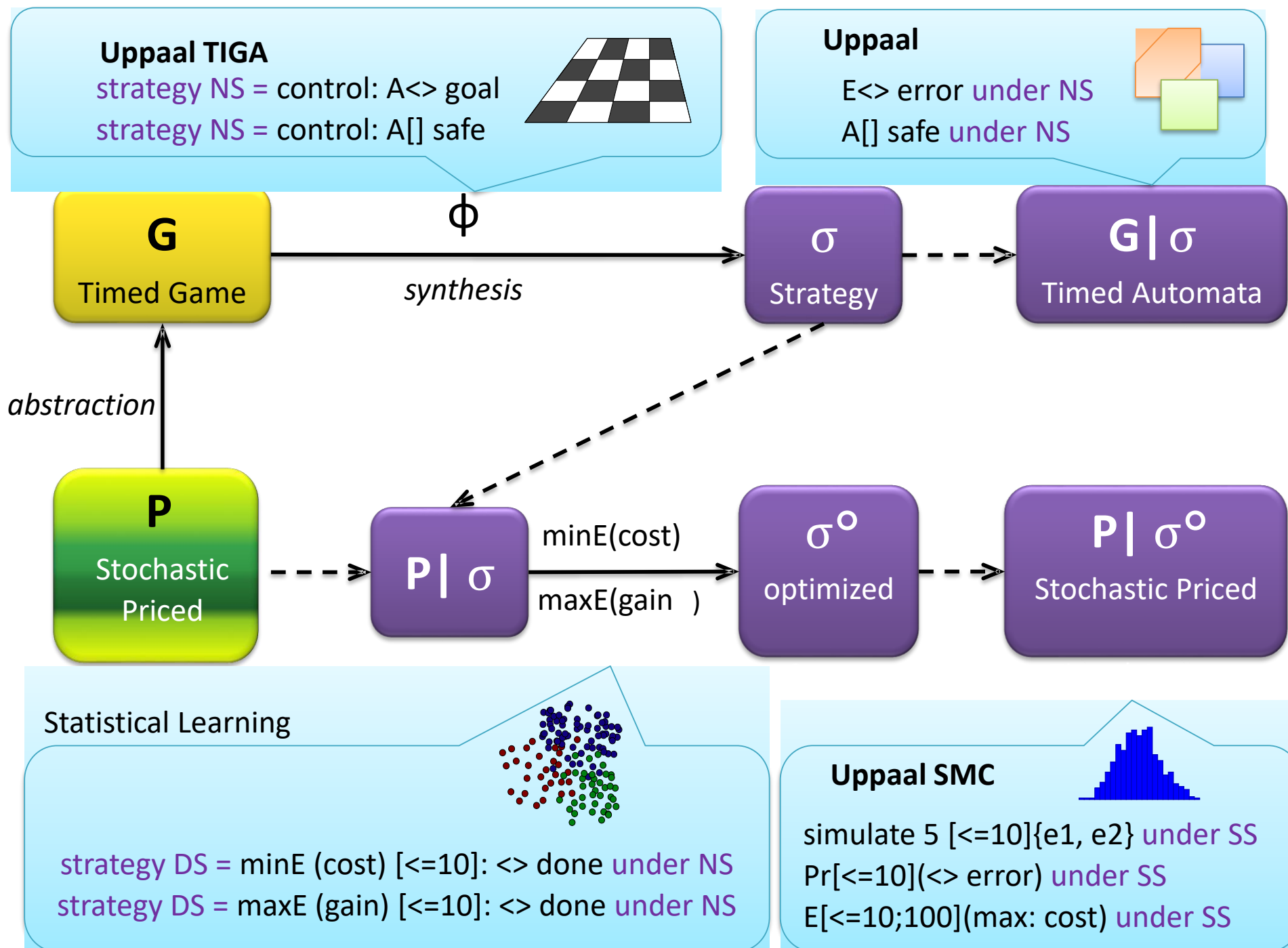


Pr[time <= 500](<> Train(5).Cross) ?

Pr[time <= 500](<> Train(0).Cross) ?



STRATEGO



HOMEWORK: PACMAN

- ≡ Create a network of timed automata
 - ≡ Ghost and Pacman
 - ≡ 3x3 grid, starting on opposite ends
 - ≡ Make the ghost edges not controllable
 - ≡ Both can stay at most 5 time units on the same field
 - ≡ Leaving a field can be done after a minimum of 2 time units

- ≡ Queries:
 - ≡ Can Pacman and Ghost be on the same grid?
 - ≡ Will they always be on different grids?
 - ≡ Can you make a strategy that lets the Pacman always escape? => if so, simulate via concrete simulator

- ≡ Allow pacman to stay for 50 instead of 5 time units, repeat the queries.
- ≡ Add a second ghost template (parametrized?)

- ≡ Hints: grid as locations or via variables? Either way, having a global variable with the current location makes the query a lot easier.
- ≡ You can combine select field and function for guard
- ≡ Use the demo folder of UPPAAL to figure out the right syntax of elements ;)

SOME EXAMPLES

≡ Grundfos pump controller

≡ Train station

≡ Brick Sorter

≡ RT OS

UNFOLD THE FUTURE

WWW.SILICON-AUSTRIA-LABS.COM